Parity-Violating Electron Scattering

Krishna Kumar, UMass Amherst Ecole Internationale Joliot-Curie Lacanau, France (26 Sep. – 2 Oct. 2010)

A unique probe of strange quarks in nucleons and the neutron skin of a heavy nucleus

Lecture 1

Outline of Lectures

Lecture 1

Symmetries and Conservation Laws

- Weak Interactions and the unified Electroweak Interactions
- Quantum Electrodynamics and Electron Scattering
- Parity-violating Electron Scattering

Lecture 2

- Strange Quark Form Factors
- Neutron skin of a heavy nucleus
- Future of parity-violating electron scattering

Introductory Remarks

Student background and preparation varies

- Most of you will have had nuclear and/or particle physics at an advanced level but I decided not to assume it.
- I have some slides on basic undergraduate and graduate subatomic physics
- As postdoctoral researchers, you will learn to cope with imperfect knowledge
 - Qualitative rather than quantitative understanding
 - I am an experimentalist! I will focus on measurements but theory is critical. Unfortunately, I wont have time to justice to it.

I will try to communicate the "big picture"

necessary general knowledge for students focused on other subfields

Parity-violating electron scattering

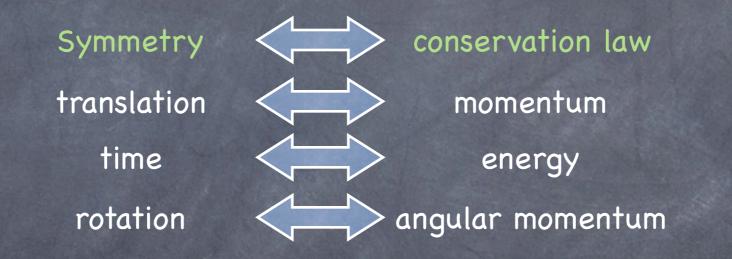
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Parity Symmetry

Symmetries and Conservation Laws

Noether's Theorem:

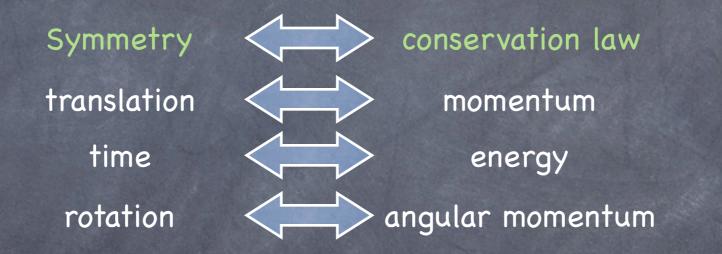
If Euler-Lagrange equation is invariant under any coordinate transformation, \exists an integral of motion



Symmetries and Conservation Laws

Noether's Theorem:

If Euler-Lagrange equation is invariant under any coordinate transformation, \exists an integral of motion



Not just space-time symmetries: Invariance of Lagrangian/Hamiltonian e.g. Charge Conservation [Q,H]=0 $\frac{d < Q >}{dt}=0$ $Q|\Psi>=q|\Psi>$

Conserved Quantities/Quantum Numbers

Parity-violating electron scattering

Symmetries and Groups

Symmetry operations:

Group of all operations: display closure & Associativity and have identity and inverse

Finite Group Infinite Group Continuous Symmetry

In Physics, group operations can be represented by matrices SO(n): n-D rotations SO(3) ←→ SU(2) Invariance under SU(2): Angular Momentum Conservation

Parity-violating electron scattering

Discrete Symmetries C, P & TParity P $x, y, z \rightarrow -x, -y, -z$ $P\psi(\vec{r}) = \psi(-\vec{r})$ $P^2 = I$ Group has 2 elements, P and I $[H, P] = 0 \longrightarrow H\psi = E\psi \& P\psi = \pi\psi \implies \pi = \pm 1$

If hamiltonian is invariant under parity transformations, then π is conserved and observable

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Parity-violating electron scattering

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A Guiding Principle for Experimentalists If a process is not explicitly forbidden, it must occur! Discovering a rare process that violates a known symmetry is a powerful way to probe the fundamental laws of nature Lepton Number Violation and Neutrinoless Double-Beta decay T-Violation and the Electric Dipole Moment of elementary particles Nuclear and Atomic Systems are fertile hunting grounds! Parity-violating electron scattering Krishna Kumar, J-C School Lecture 1, Sep 30 2010 8

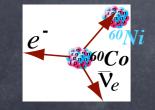
Discovery of Discovery of Parity Violation Particle Classification S^{π} e.g. pions: 0^{-} pseudoscalar mesons Tau-theta puzzle (1956) $\theta^{+} \rightarrow \pi^{+}\pi^{0}$ (P=+1) $\tau^{+} \rightarrow \pi^{+}\pi^{0}\pi^{0}$ (P=-1)

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P conserved in strong interactions, but not in weak interactions

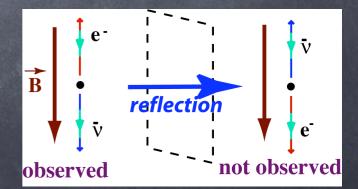
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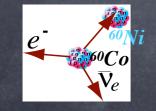
Weak decay of ⁶⁰Co Nucleus

C.S. Wu et al: Beta's in decays of ⁶⁰Co nuclei aligned in a magnetic field showed anisotropy



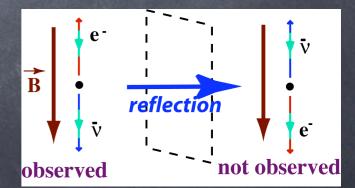
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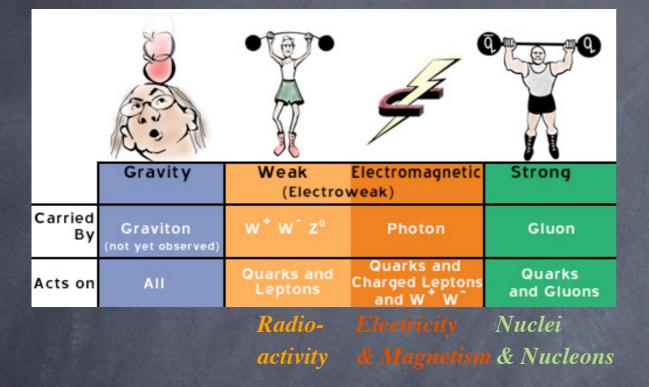
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Classic example: Puzzle in accelerator result; theorists propose a solution; test on a different process (table-top)

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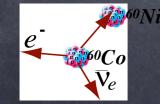


Gravity and Electromagnetic Infinite range

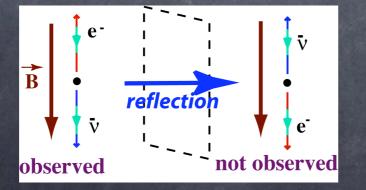
> Strong and Weak 10⁻¹⁵ meter



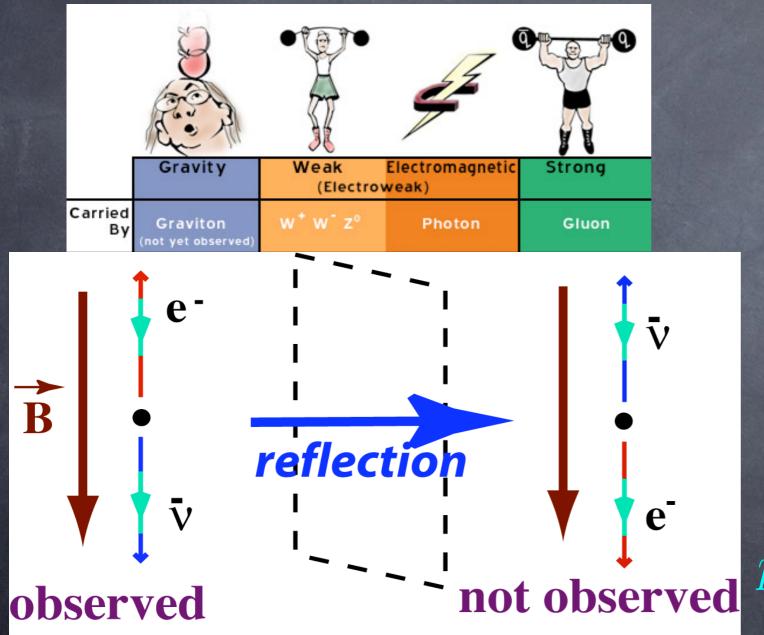
 $egin{aligned} & x,y,z
ightarrow -x,-y,-z \ & ec{p}
ightarrow -ec{p}, \ ec{L}
ightarrow ec{L}, \ ec{s}
ightarrow ec{s} \end{aligned}$



Weak decay of ⁶⁰Co Nucleus



Parity-violating electron scattering

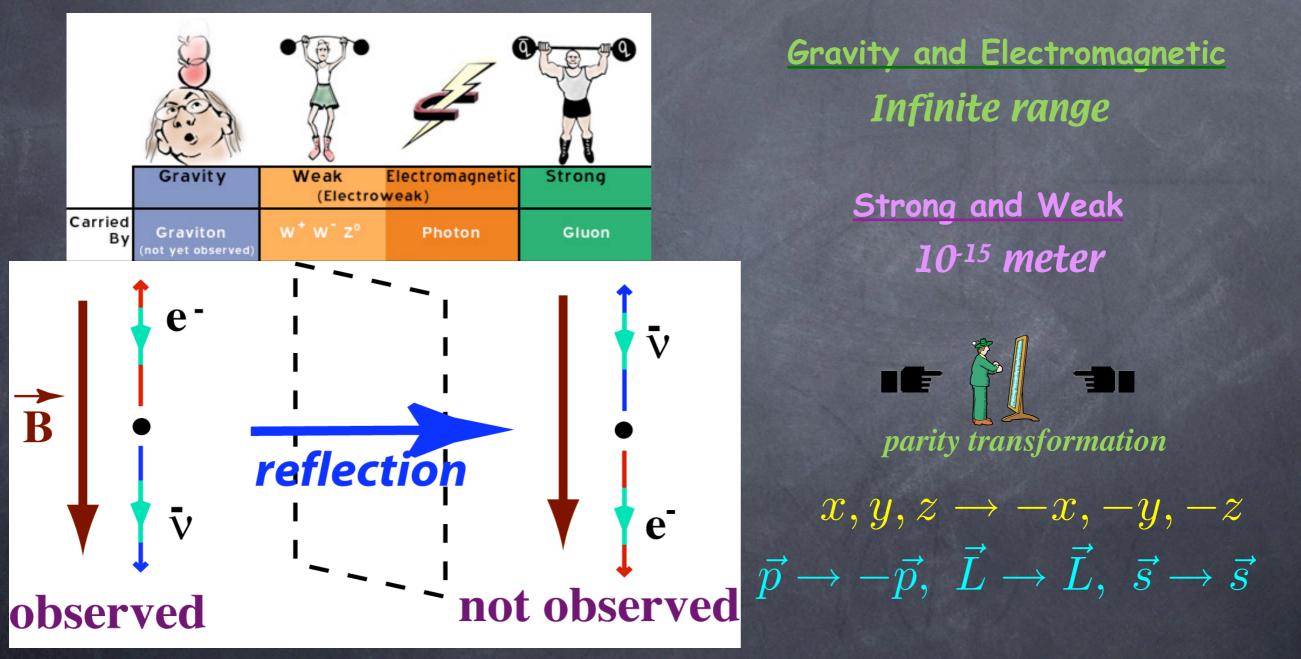


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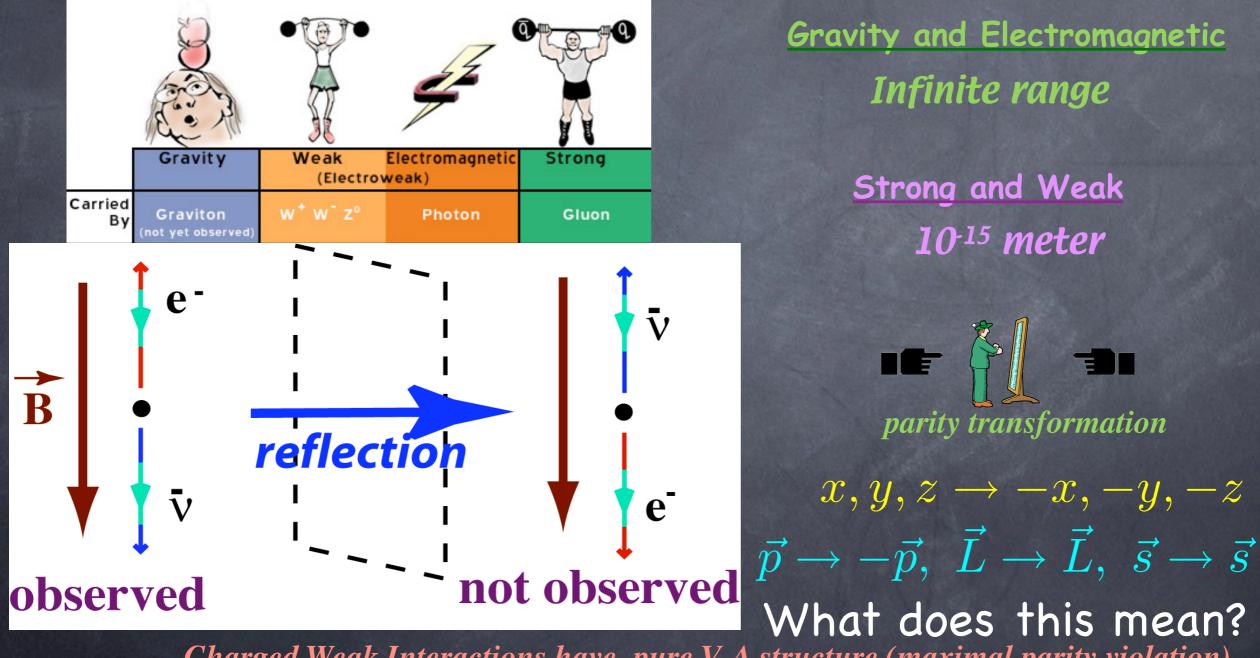


 $x, y, z \rightarrow -x, -y, -z$ $ec{p} \rightarrow -ec{p}, \ ec{L} \rightarrow ec{L}, \ ec{s} \rightarrow ec{s}$



Charged Weak Interactions have pure V-A structure (maximal parity violation)

Parity-violating electron scattering



Gravity and Electromagnetic Infinite range

> Strong and Weak 10-15 meter

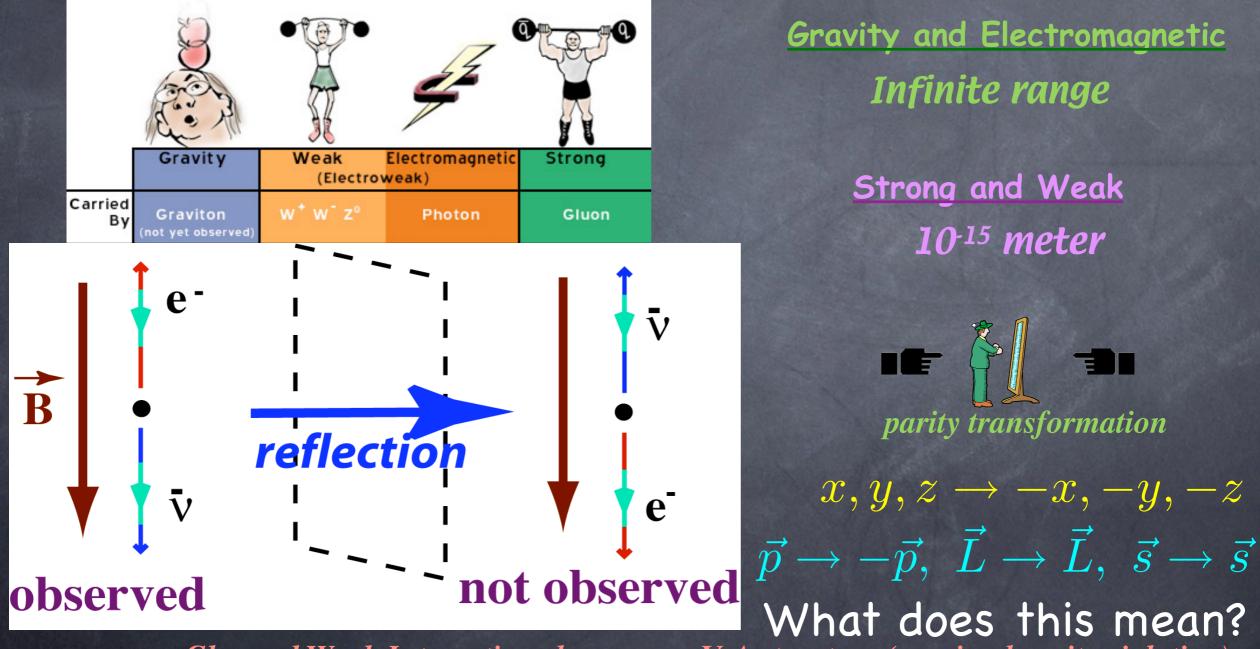


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Parity-violating electron scattering

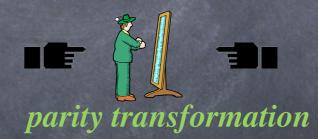
Why are weak interactions short range?

Fundamental Interactions



Gravity and Electromagnetic Infinite range

> Strong and Weak 10-15 meter



x, y, z
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What does this mean?

Charged Weak Interactions have pure V-A structure (maximal parity violation)

Parity-violating electron scattering

Why are weak interactions short range?

Gravity

Graviton

e -

et observed

Carried

observed

B

By

Weak

(Electroweak)

reflection

Electromagnetic

Photon

Strong

Gluon

Fundamental Interactions

How are weak and EM interactions unified given P-Violation?

Gravity and Electromagnetic Infinite range

> Strong and Weak 10⁻¹⁵ meter



 $x, y, z \rightarrow -x, -y, -z$

What does this mean?

 $\vec{p} \rightarrow -\vec{p}, \vec{L} \rightarrow \vec{L}, \vec{s} \rightarrow \vec{s}$

Charged Weak Interactions have pure V-A structure (maximal parity violation)

Parity-violating electron scattering

e

not observed

Continuous SymmetriesDirac free particle $\mathcal{L} = \bar{\psi}(i\gamma^{\mu}\partial_{\mu} - m)\psi$ LagrangianU(1) Invariance: conserved current $\partial_{\mu}J^{\mu} = 0$

Local U(1) Invariance: $A_{\mu}J^{\mu}$ Electromagnetic Interactions

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Rotation in $\begin{pmatrix} p \\ n \end{pmatrix}$ nucleon-nucleon interaction Hamiltonian invariant
under SU(2) transformations in Isospin Space"Isospin Space" $\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L$ the "massless" left-handed electron and electron-
neutrino are part of a similar "weak isospin" doublet

SU(2) invariance yields 3 independent conserved currents

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(there are 3 independent 2x2 Pauli spin matrices)

Symmetries of the Electroweak Lagrangian Accept the existance of u & d quarks, electrons, and electron-neutrinos $SU(2)_L \times U(1)_Y$ Local gauge invariance yields 4 bosons: W⁺, W⁻, W⁰, B⁰

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 Z^0

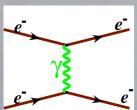
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Electroweak Interactions

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Electric charge determines strength of electric force

Electrons and protons have same charge magnitude: same strength

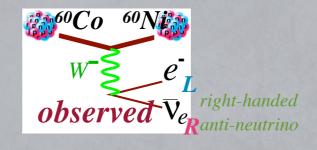


Neutrinos are "charge neutral": do not feel the electric force not observed

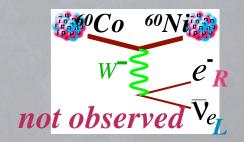
observed

Weak charge determines strength of weak force

Left-handed particles (Right-handed antiparticles) have weak charge



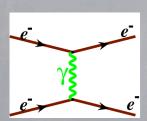
Right-handed particles (left-handed antiparticles) are "weak charge neutral"



left-handed anti-neutrino

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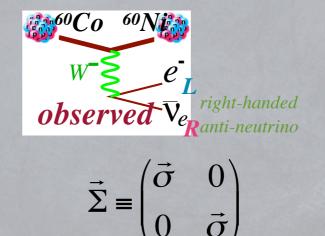
observed

For massless particles: $\gamma^5 u$

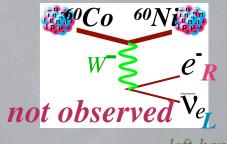
$$\gamma^5 \mu = (\vec{n} \bullet \vec{\Sigma}) \mu$$

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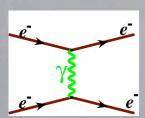
 $\vec{p} \bullet \vec{\Sigma} \equiv h$ left-handed anti-neutrino

helicity operator

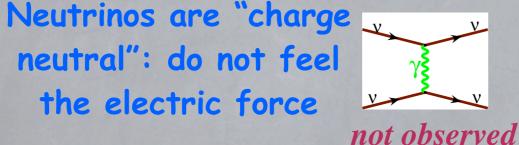
Parity-violating electron scattering

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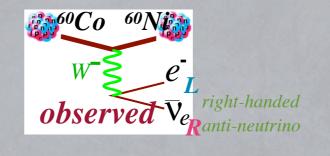


observed



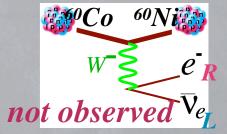
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 $\vec{\Sigma} \equiv \begin{pmatrix} \vec{\sigma} & 0 \\ 0 & \vec{\sigma} \end{pmatrix}$

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left-handed anti-neutrino

helicity operator

 $\vec{p} \bullet \Sigma \equiv h$

$$\Sigma u = -u \quad \Box \rangle \frac{(1-\gamma^5)}{2}u = u$$

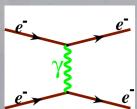
For massless particles: $\gamma^5 u = (\vec{p} \bullet \vec{\Sigma}) u$

$$\Sigma u = + u \, \square \rangle \, \frac{(1 - \gamma^5)}{2} u = 0$$

Parity-violating electron scattering

Electric charge determines strength of electric force

Electrons and protons have same charge magnitude: same strength



observed

For massless particles:

$$\Sigma u = + u \, \Box \rangle \, \frac{(1 - \gamma^5)}{2} u = 0$$

 $\gamma^5 u = (\vec{p} \bullet \vec{\Sigma}) u$

$$P_L = \frac{(1 - \gamma^5)}{2} \quad P_R = \frac{(1 + \gamma^5)}{2}$$

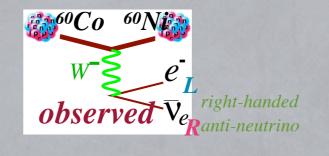
Left- and right-handed projections

$$P_{L,R} u \equiv u_{L,R}$$
 $P_i P_j = \delta_{ij} P_j$ $\sum_i P_i =$

Parity-violating electron scattering

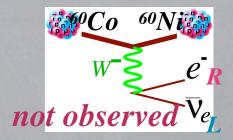
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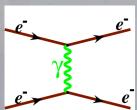
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Electric charge determines strength of electric force

Electrons and protons have same charge magnitude: same strength



observed

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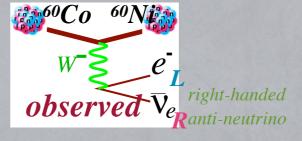
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Parity-violating electron scattering

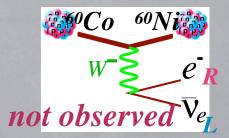
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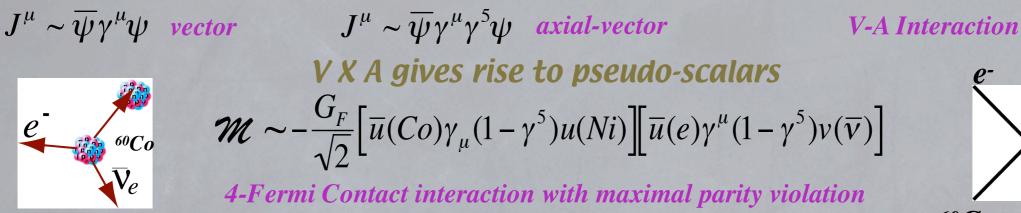
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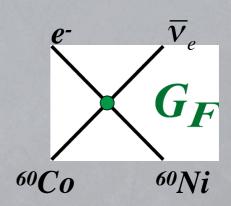
$$-\frac{G_F}{\sqrt{2}} \Big[\overline{u}_L(Co) \gamma_\mu u_L(Ni) \Big] \Big[\overline{u}_L(e) \gamma^\mu v_R(\overline{v}) \Big]$$

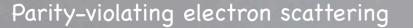
Only left-handed particles participate in charged weak interactions

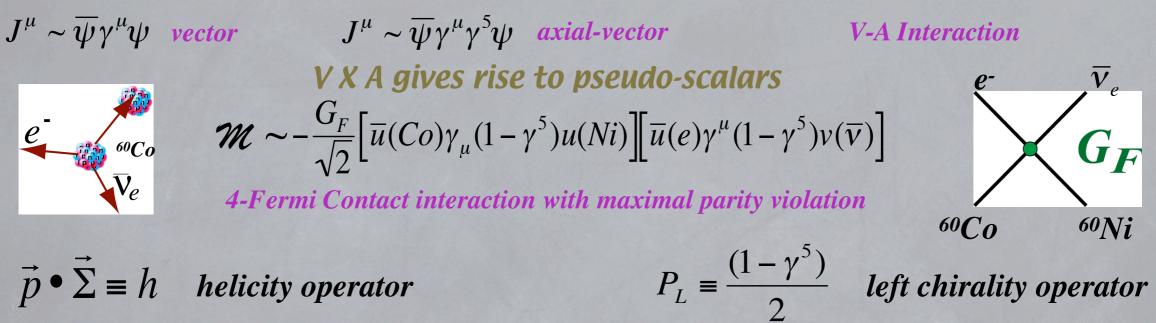
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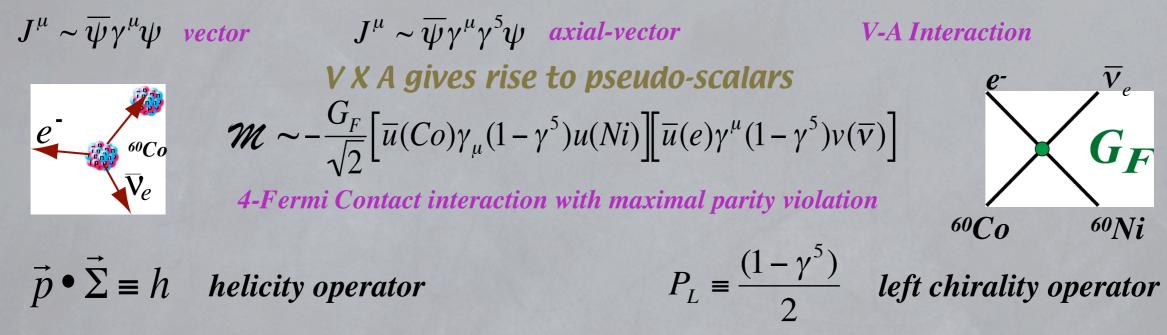






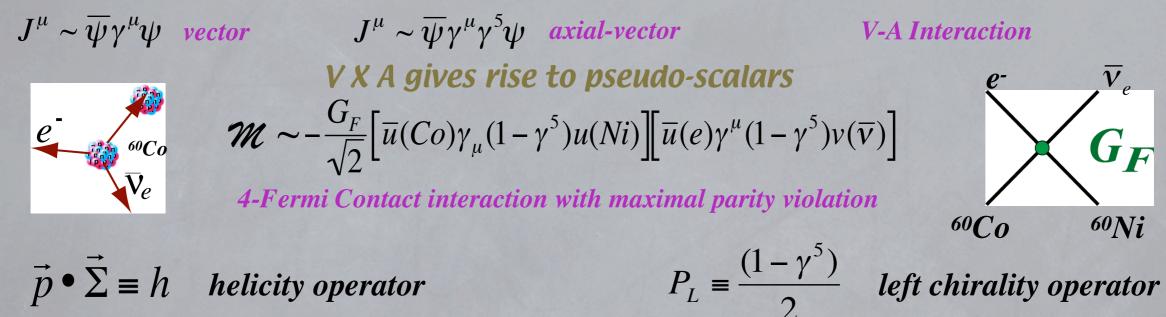


Important: Helicity ≠ *Chirality if m*≠0!



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Parity-violating electron scattering



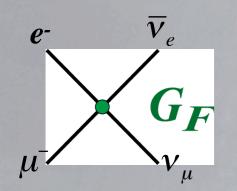
Important: Helicity ≠ Chirality if m≠0! Helicity operator commutes with free-particle Hamiltonian Conserved but not Lorentz invariant! (Can race past a massive particle and observe it spinning the other way)

Chirality operator not conserved, but Lorentz invariant!

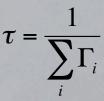
Freely propagating left-chiral projection will develop a right-chiral component

Parity-violating electron scattering

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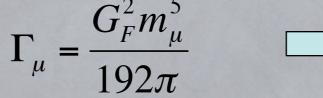
Lifetime



Each decay mode provides a partial width Γ_i

 $\begin{aligned} & \mathcal{S} cattering \\ & \mathcal{M} \sim -\frac{G_F}{\sqrt{2}} \Big[\bar{u}(v_{\mu}) \gamma_{\mu} (1-\gamma^5) u(\mu) \Big] \Big[\bar{u}(e) \gamma^{\mu} (1-\gamma^5) v(\bar{v}_e) \Big] \end{aligned}$

Partial width has units of energy $C^2 m^5$

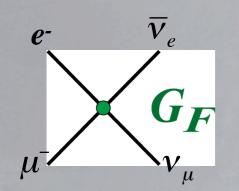


Conversion factor: 197 MeV-fm

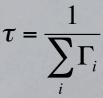
Muon lifetime in vacuum: 2.2 µs

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Partial width has units of energy

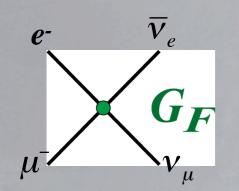
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Gedanken Experiments: The luxury of being a theorist

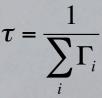
Consider **Can use same** \mathcal{M} $\sigma = \frac{G_F E^2}{2 \sigma^2}$ $\overline{v}_e + e^- \rightarrow \overline{v}_\mu + \mu^-$

 $\begin{aligned} & \mathcal{S} cattering \\ & \mathcal{M} \sim -\frac{G_F}{\sqrt{2}} \Big[\overline{u}(v_{\mu}) \gamma_{\mu} (1-\gamma^5) u(\mu) \Big] \Big[\overline{u}(e) \gamma^{\mu} (1-\gamma^5) v(\overline{v}_e) \Big] \end{aligned}$

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Partial width has units of energy

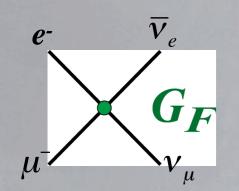
Conversion factor: 197 MeV-fm

Gedanken Experiments: The luxury of being a theorist $\sigma = \frac{G_F^2 E^2}{2}$

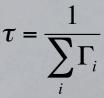
Consider $\overline{v}_e + e^- \rightarrow \overline{v}_u + \mu^-$

Each decay mode provides a partial width Γ_i

 $\mathcal{M} \sim -\frac{G_F}{\sqrt{2}} \left[\overline{u}(v_{\mu}) \gamma_{\mu} (1 - \gamma^5) u(\mu) \right] \left[\overline{u}(e) \gamma^{\mu} (1 - \gamma^5) v(\overline{v}_e) \right]$



Lifetime



Partial width has units of energy

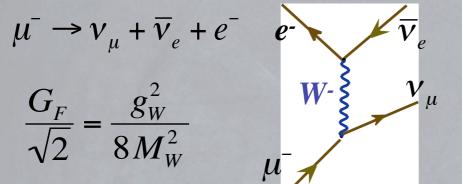
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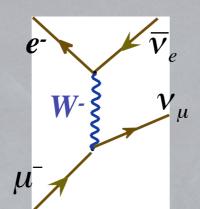
Gedanken Experiments: The luxury of being a theorist

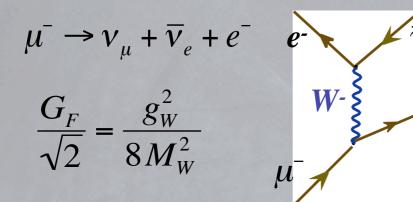
Can use same \mathcal{M} $\sigma = \frac{G_F^2 E^2}{2 r^2}$ Consider $\overline{v}_e + e^- \rightarrow \overline{v}_\mu + \mu^-$

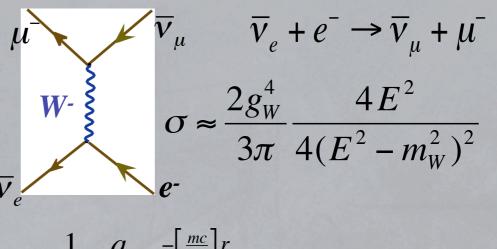
For $E \sim 1$ TeV, probability > 1!

More particles going out than coming in



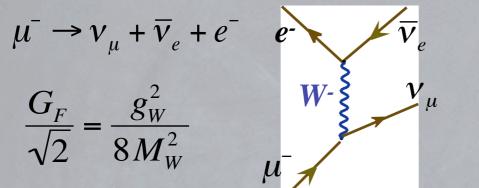


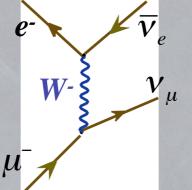


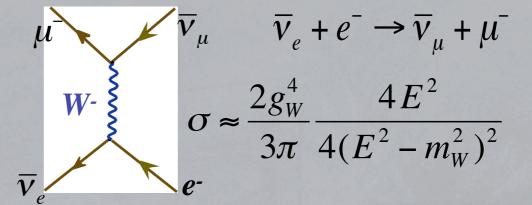


Mass of the W between 10 and 100 GeV

 $V = \frac{1}{4\pi\varepsilon_0} \frac{q}{r} e^{-\left[\frac{mc}{\hbar}\right]r}$ Short range







Mass of the W between 10 and 100 GeV

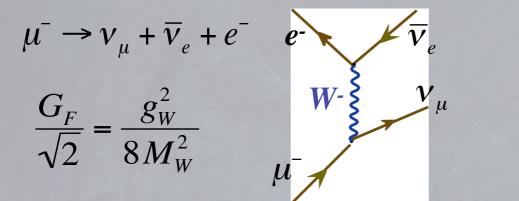
$$V = \frac{1}{4\pi\varepsilon_0} \frac{q}{r} e^{-\left[\frac{mc}{\hbar}\right]r} \qquad Short range$$

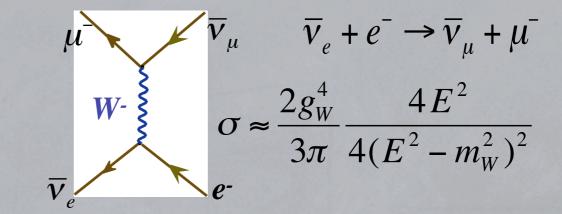
Real W production

Fixed target: $M^2_{new} \sim 2ME$

 $u + \overline{d} \rightarrow W^+ \rightarrow e^+ + v_e$

Collider: $M_{new}^2 \sim 4E^2$





Mass of the W between 10 and 100 GeV

$$V = \frac{1}{4\pi\varepsilon_0} \frac{q}{r} e^{-\lfloor\frac{\pi}{\hbar}\rfloor^r} \qquad Short range$$

[mc]

Real W production

 $u + \overline{d} \rightarrow W^+ \rightarrow e^+ + v_e$

Fixed target: $M^2_{new} \sim 2ME$

Collider: $M_{new}^2 \sim 4E^2$

Very short lifetime $\langle - \rangle$ Large width

 $p(E) = \frac{\Gamma}{2\pi} \frac{1}{(E - m_W)^2 + (\Gamma/2)^2}$

Parity-violating electron scattering

 $A + B \rightarrow W^+ \rightarrow C + D$

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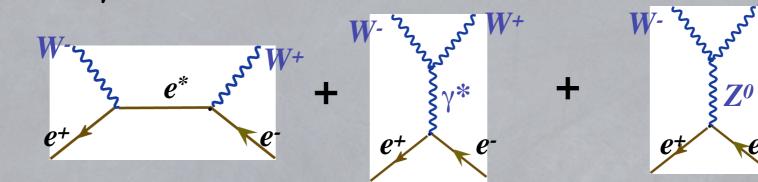
 $\sigma_{peak} \approx \frac{4\pi}{3m^2} \frac{\Gamma_{AB}}{\Gamma} \frac{\Gamma_{CD}}{\Gamma}$

The Z Boson & Electroweak Unification

More gedanken experiments

 $e^+ v_{\rho} \rightarrow W^+ \gamma$

Electron-positron collisions $e^+e^- \rightarrow W^+W^-$

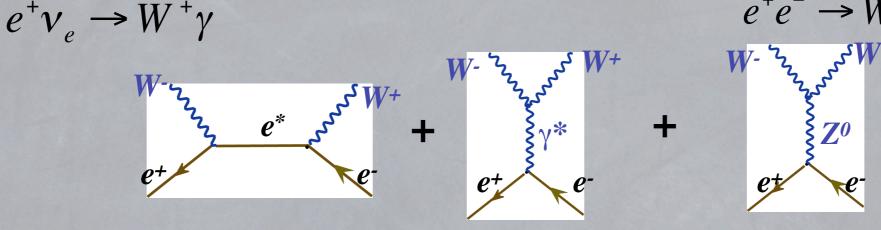


Unitarity violation forces important constraints
Need WW_γ vertex: same charge as electron!
Need a new, neutral massive weak boson: the Z⁰
One free parameter: θ_w, the weak mixing angle

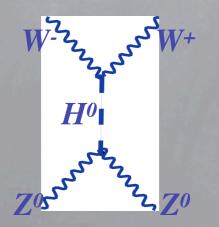
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Scattering of longitudinal vector bosons (m=0)

•eeZ couplings depend on $\sin^2 \theta_W$

$$\frac{m_W}{m_Z} = \cos\theta_W$$

Parity-violating electron scattering

Ζ.

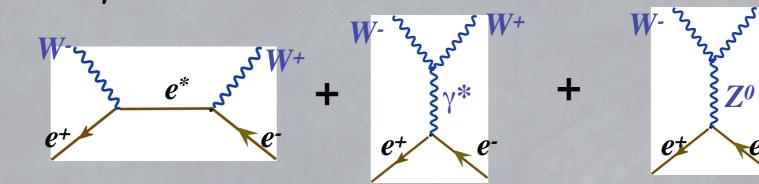
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The Z Boson & Electroweak Unification

More gedanken experiments

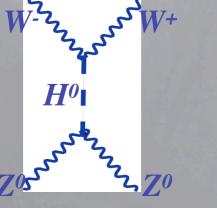
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Unitarity violation forces important constraints
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Something like this must occur



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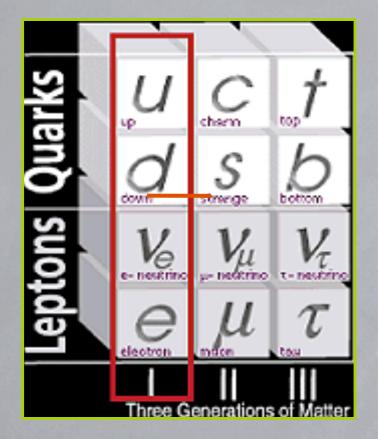
Parity-violating electron scattering

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Ζ.

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W & Z Charges



Left-handed particles in isodoublets
Right-handed particles iso-singlets
Including neutrinos!

	Left-	Right-
γ Charge	$q = 0, \pm 1, \pm \frac{1}{3}, \pm \frac{2}{3}$	$q = 0, \pm 1, \pm \frac{1}{3}, \pm \frac{2}{3}$
W Charge	$T = \pm \frac{1}{2}$	T = 0
Z Charge	$T-q\sin^2\theta_W$	$-q\sin^2\theta_W$

- •Ws and Zs are massive
- •Ws have no couplings to right-handed particles
- •Zs couple to both (provided the particles are charged): introduce g_L and g_R •However, the Z couplings to left- and right-handed particles are different: parity violation, but not maximal

Also use g_V and g_A :

 $g_V = g_L + g_R$ $g_A = g_L - g_R$ Vector and Axial-vector couplings

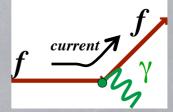
Electron Scattering

Free fermions fields are solutions to the Dirac equation $(i\gamma_{\mu}\partial^{\mu} - m)\psi = 0$ *Corresponding Lagrangian:* $\mathcal{L} \sim \overline{\psi}(i\gamma_{\mu}\partial^{\mu} - m)\psi$

 $-J_{\mu}A^{\mu}$

Local gauge invariance gives rise to interaction with photon field: Conserved electromagnetic current $J^{\mu} = q \overline{\psi} \gamma^{\mu} \psi \quad 4\text{-vector}$

Feynman Rules: emission and absorption of virtual photons by fermion electromagnetic current

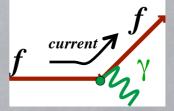


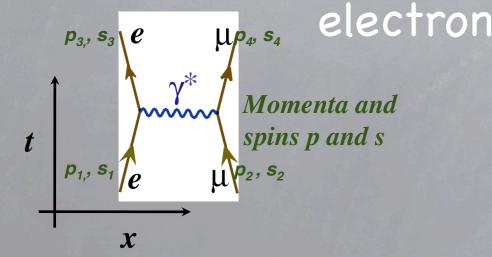
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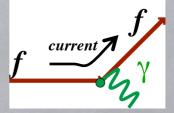
electron-muon scattering

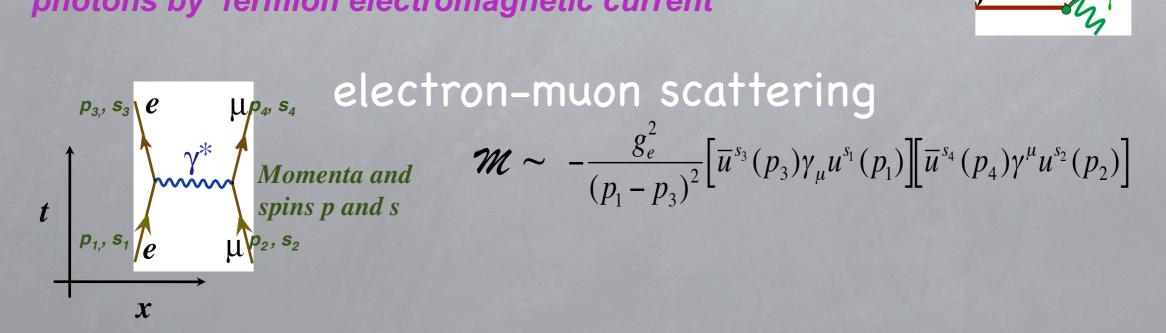
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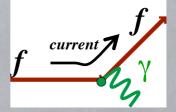
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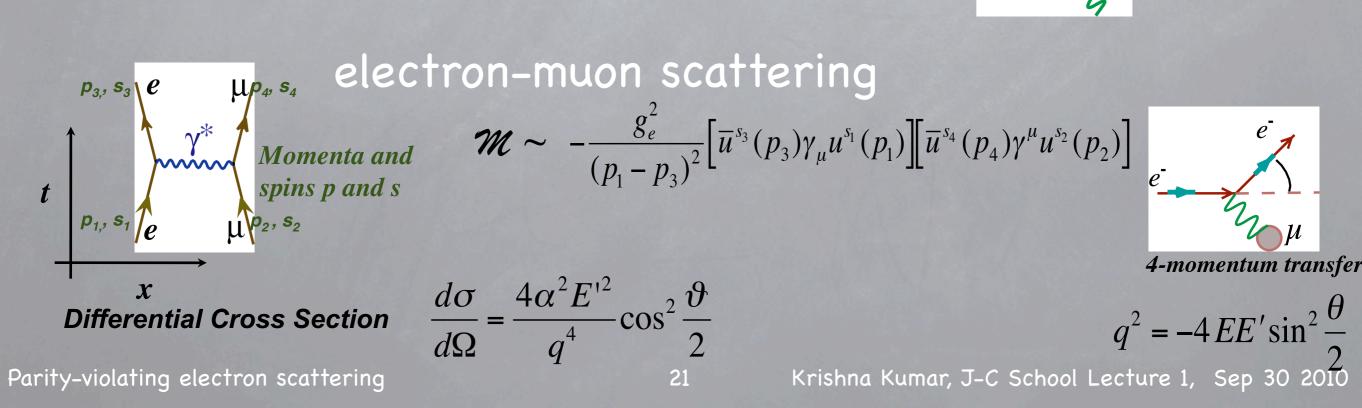
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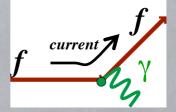


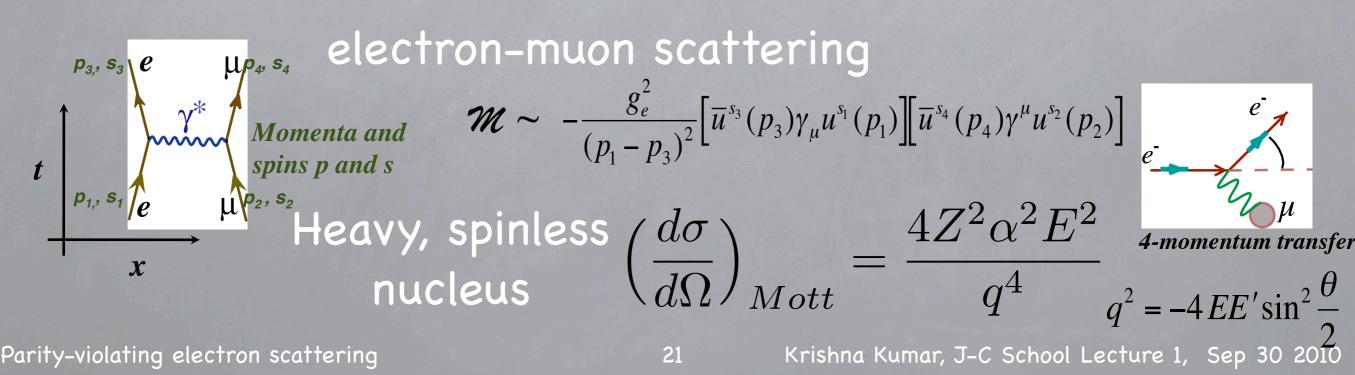
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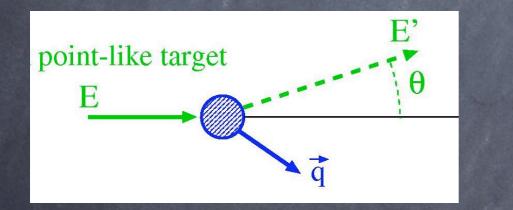


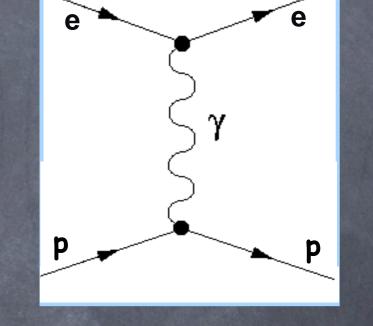
Electromagnetic Probe of Hadron Matter

 $Q \approx \frac{hc}{2}$

Electron scattering: electromagnetic interaction, described as an exchange of a virtual photon.

If photon carries low momentum -> long wavelength -> low resolution





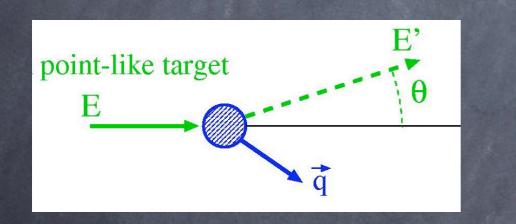
Q²: 4-momentum of the virtual photon

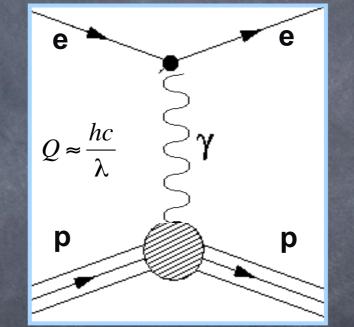
Increasing momentum transfer -> shorter wavelength -> higher resolution to observe smaller structures

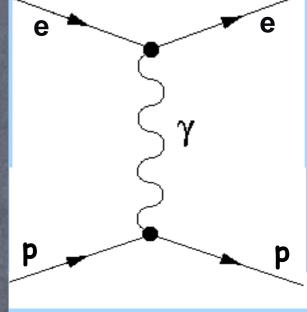
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P P P

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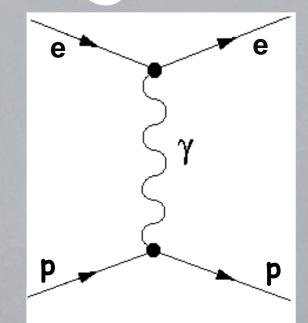
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Elastic e-p Scattering

For a point-like target, accounting for target recoil:

Function of (E, θ) . Cross-section for infinitely heavy, fundamental target

	$T = Q^2 / 4M^2$ is a
	convenient
$rac{{ m d}\sigma}{{ m d}\Omega}=rac{{ m d}\sigma}{{ m d}\Omega}_{ m Mott}$	kinematic factor $\left\{ 1 + 2 au an^{2}(heta/2) ight\}$



Elastic e-p Scattering

For a point-like target, accounting for target recoil:

 $\mathbf{d}\sigma$

 $= \frac{\mathrm{d}\Omega}{\mathrm{d}\Omega}_{\mathrm{Mott}}$

 $\mathbf{d}\sigma$

 $\mathrm{d}\Omega$

Function of (E, θ) . Cross-section for infinitely heavy, fundamental target

If proton is not point-like: The electric and magnetic form factors G_E and G_M parameterize the effect of proton structure.

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma}{d\Omega} \underbrace{\frac{E'}{E}}_{Mott} \left\{ \underbrace{\left(G_{E}^{2} + \tau G_{M}^{2} \right)}_{1 + \tau} + 2\tau G_{M}^{2} \tan^{2}(\theta/2) \right\}}_{I + \tau}$$
If the proton were like the electron:
 $G_{E} = 1$ (proton charge)
 $G_{M} = 1$ (and the magnetic moment
would be 1 Bohr magneton).

Parity-violating electron scattering

e

 $\tau = Q^2/4M^2$ is a

kinematic factor

convenient

 $\{\mathbf{1}+\mathbf{2}\tau^{\dagger}\tan^{2}(\theta/\mathbf{2})\}$

e

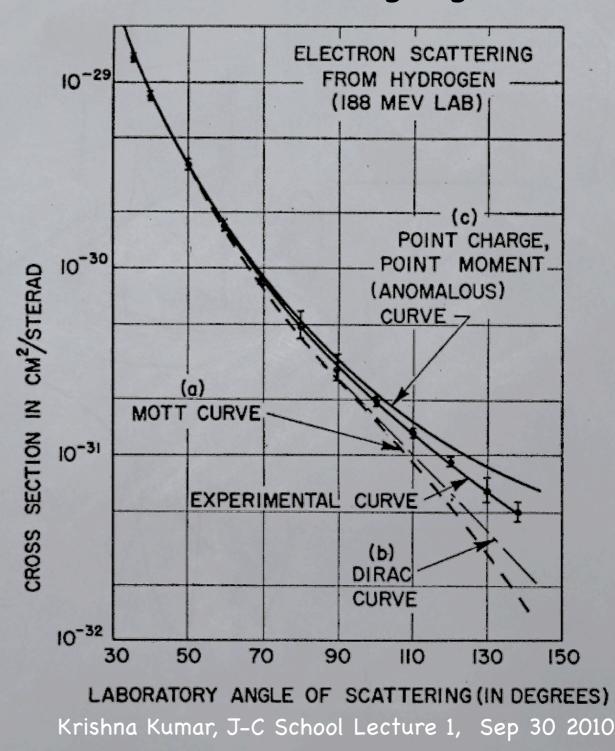
Finite Size of the Proton

Otto Stern (1932) measured the proton magnetic moment $\mu_p \sim 2.5 \mu_{Bohr}$ (first indication that the proton was not a point-like particle, Nobel prize 1943)

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Stanford U. Mark III Accelerator McAllister and Hofstadter, Physical Review 102 (1956) 851.

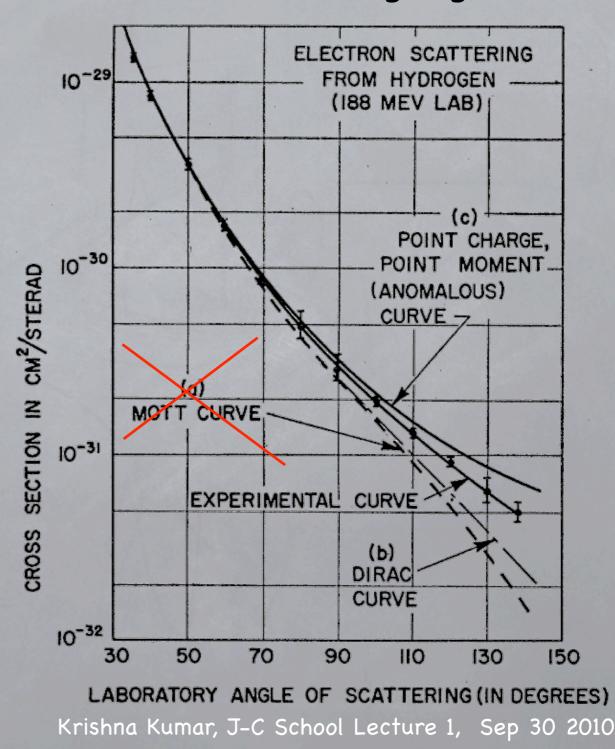
various scattering angles



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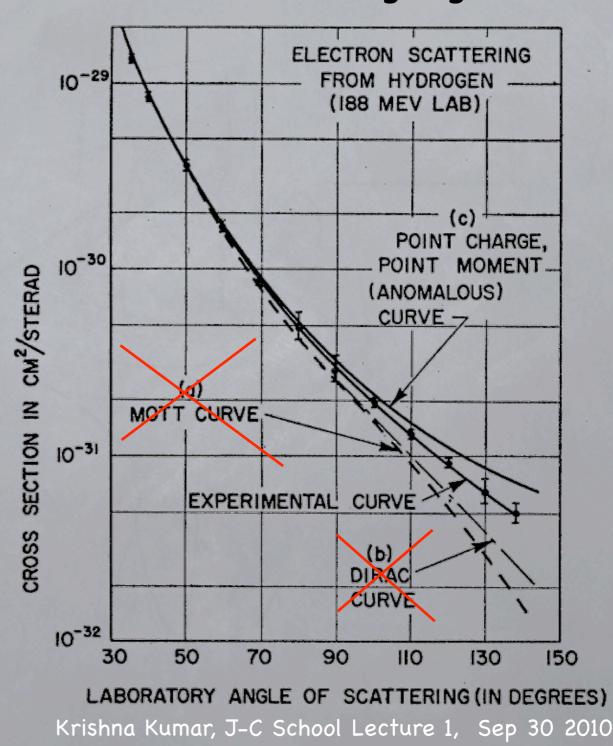


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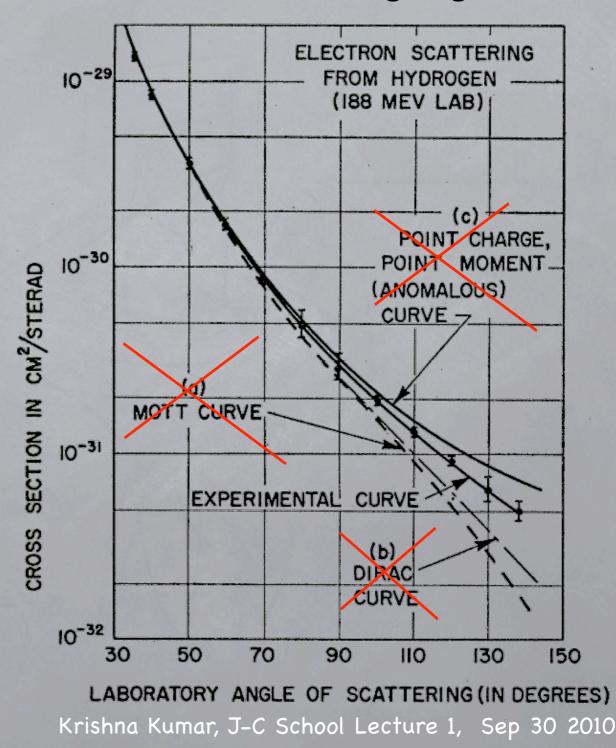
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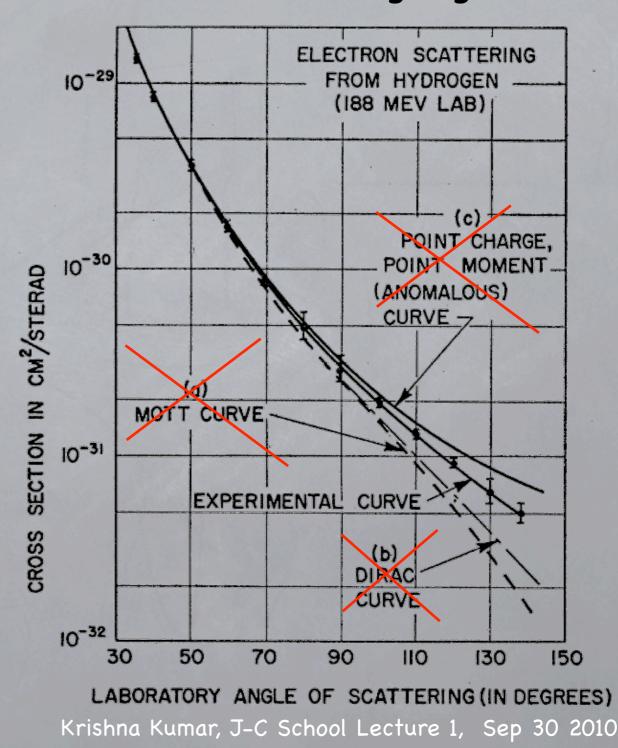
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It isn't Mott, nor Dirac, nor Rosenbluth with $G_F=1$ and $G_M=2.79...$ various scattering angles



Finite Size of the Proton

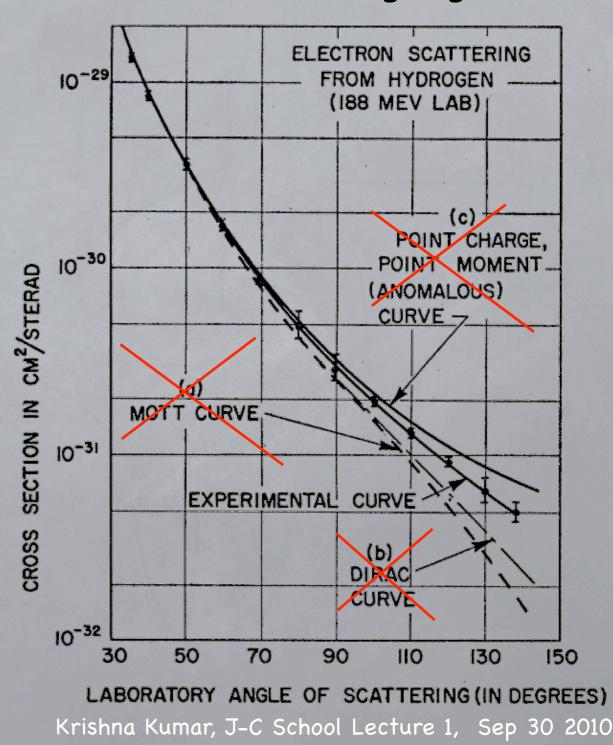
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It isn't Mott, nor Dirac, nor Rosenbluth with $G_E=1$ and $G_M=2.79...$

the proton has finite size!

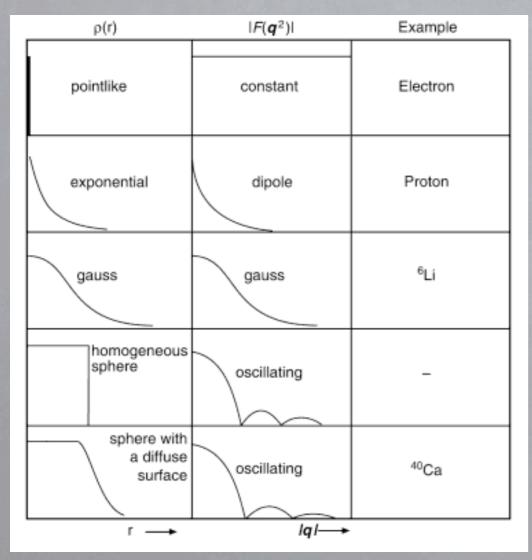
Robert Hofstadter – Noble Laureate 1961 Cross-section measurements at various scattering angles



Nuclear Size

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\rm Mott} \left|F(q)\right|^2$$

The point-like scattering probability modified: account for Finite Target Extent with a "form factor" $F(q) = \int e^{iqr} \rho(r) d^3r$ Form factor is the Fourier transform of charge distribution



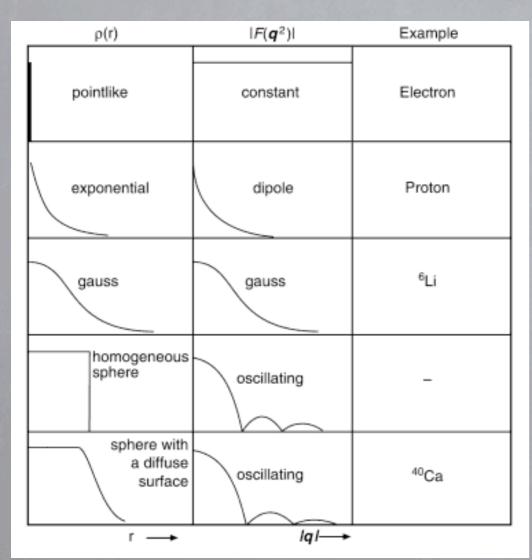
Parity-violating electron scattering

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Nuclear Size

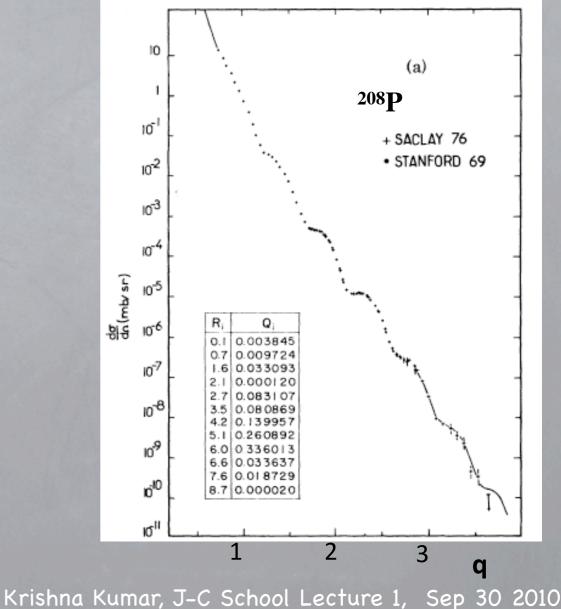
$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\rm Mott} \left|F(q)\right|$$

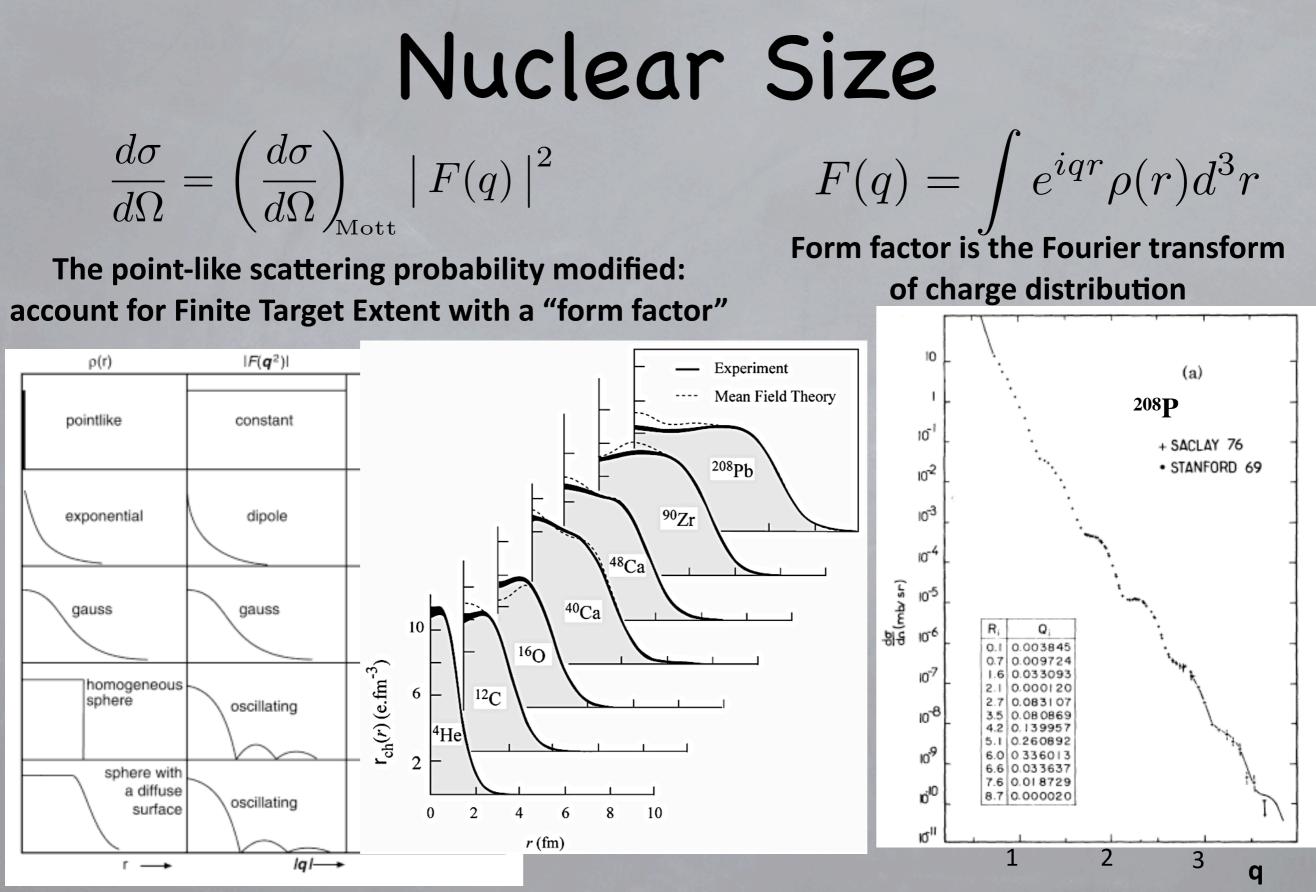
The point-like scattering probability modified: account for Finite Target Extent with a "form factor"



 $F(q) = \int e^{iqr} \rho(r) d^3r$ Form factor is the Fourier transform

Form factor is the Fourier transform of charge distribution





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Parity-violating electron scattering

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A Classic Paper

LETTERS TO THE EDITOR

PARITY NONCONSERVATION IN THE FIRST ORDER IN THE WEAK-INTER-ACTION CONSTANT IN ELECTRON SCATTERING AND OTHER EFFECTS

Ya. B. ZEL' DOVICH

Submitted to JETP editor December 25, 1958

J. Exptl. Theoret. Phys. (U.S.S.R.) 36, 964-966 (March, 1959)

Parity Violation in Electron Scattering?

(2)

WE assume that besides the weak interaction that causes beta decay,

 $g(\overline{PON})(\overline{e}^{-}Ov) + \text{Herm. conj.},$ (1)

there exists an interaction

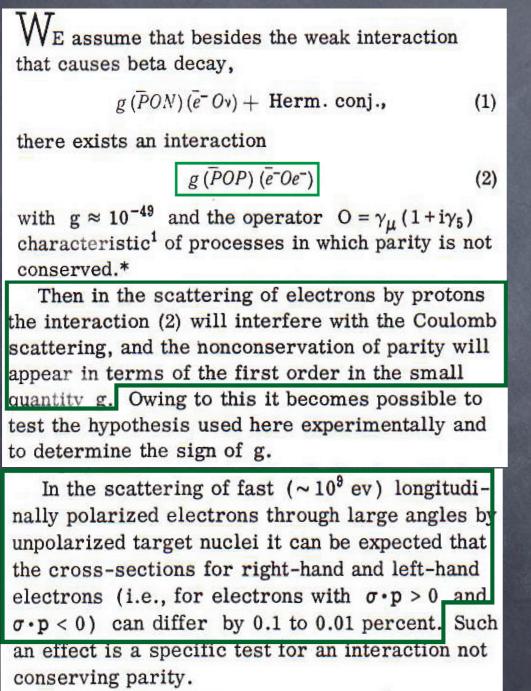
g (POP) (e^-Oe^-)

with $g \approx 10^{-49}$ and the operator $O = \gamma_{\mu} (1 + i\gamma_5)$ characteristic¹ of processes in which parity is not conserved.*

Then in the scattering of electrons by protons the interaction (2) will interfere with the Coulomb scattering, and the nonconservation of parity will appear in terms of the first order in the small quantity g. Owing to this it becomes possible to test the hypothesis used here experimentally and to determine the sign of g.

In the scattering of fast $(\sim 10^9 \text{ ev})$ longitudinally polarized electrons through large angles by unpolarized target nuclei it can be expected that the cross-sections for right-hand and left-hand electrons (i.e., for electrons with $\sigma \cdot \mathbf{p} > 0$ and $\sigma \cdot \mathbf{p} < 0$) can differ by 0.1 to 0.01 percent. Such an effect is a specific test for an interaction not conserving parity.

Parity Violation in Electron Scattering?



Neutron β Decay $V \longrightarrow \stackrel{e}{G_F} \xrightarrow{e} \stackrel{e}{p} \xrightarrow{e} \stackrel{e}{G_F} \stackrel{e}{g}$

Parity-violating electron scattering

Krishna Kumar, J-C School Lecture 1, Sep 30 2010

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 $g(\overline{PON})(\overline{e}^{-}Ov) + \text{Herm. conj.},$ (1)

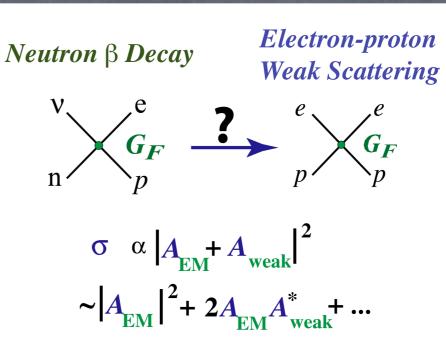
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$$g(\overline{P}OP)(\overline{e}^{-}Oe^{-})$$
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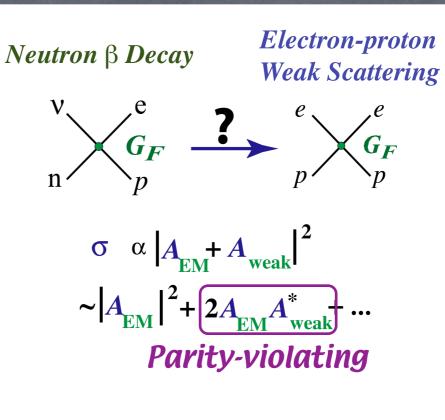
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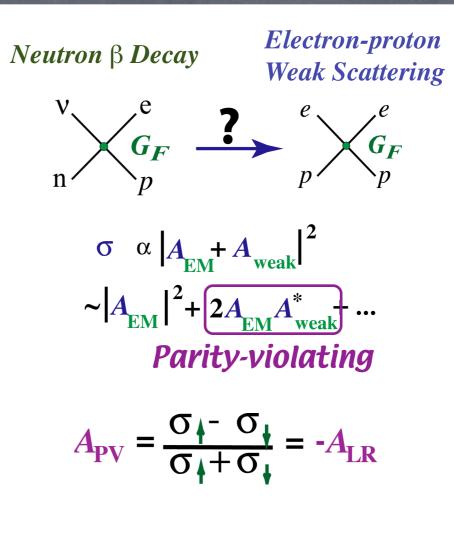
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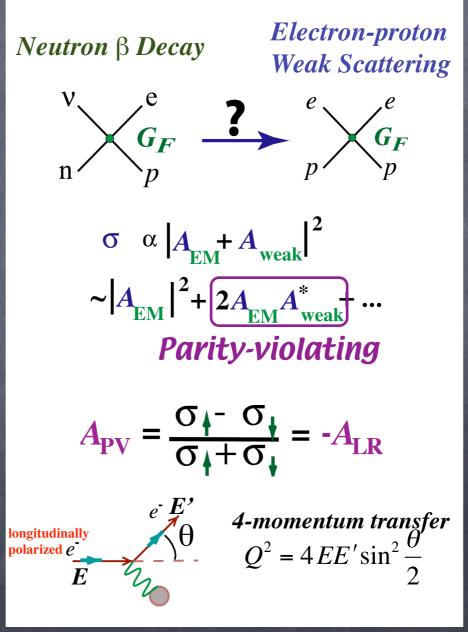
Then in the scattering of electrons by protons the interaction (2) will interfere with the Coulomb scattering, and the nonconservation of parity will appear in terms of the first order in the small quantity g. Owing to this it becomes possible to test the hypothesis used here experimentally and to determine the sign of g.

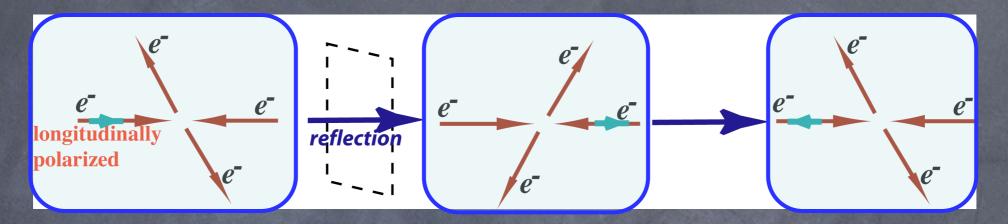
In the scattering of fast ($\sim 10^9$ ev) longitudinally polarized electrons through large angles by unpolarized target nuclei it can be expected that the cross-sections for right-hand and left-hand electrons (i.e., for electrons with $\sigma \cdot p > 0$ and $\sigma \cdot p < 0$) can differ by 0.1 to 0.01 percent. Such an effect is a specific test for an interaction not conserving parity.

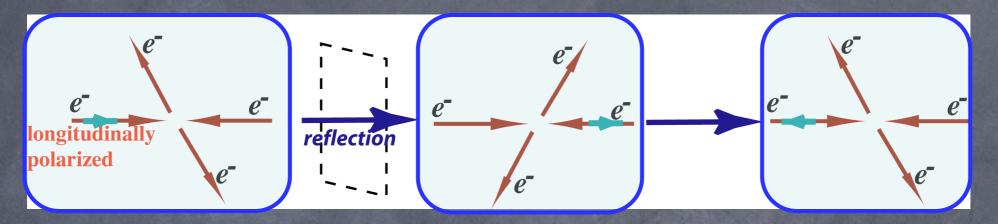


 W_E assume that besides the weak interaction that causes beta decay, $g(\overline{PON})(\overline{e}^{-}Ov) + \text{Herm. conj.},$ (1) there exists an interaction g (POP) (e-Oe-) (2)with $g \approx 10^{-49}$ and the operator $O = \gamma_{\mu} (1 + i\gamma_5)$ characteristic¹ of processes in which parity is not conserved.* Then in the scattering of electrons by protons the interaction (2) will interfere with the Coulomb scattering, and the nonconservation of parity will appear in terms of the first order in the small quantity g. Owing to this it becomes possible to test the hypothesis used here experimentally and to determine the sign of g. In the scattering of fast (~ 10^9 ev) longitudinally polarized electrons through large angles by

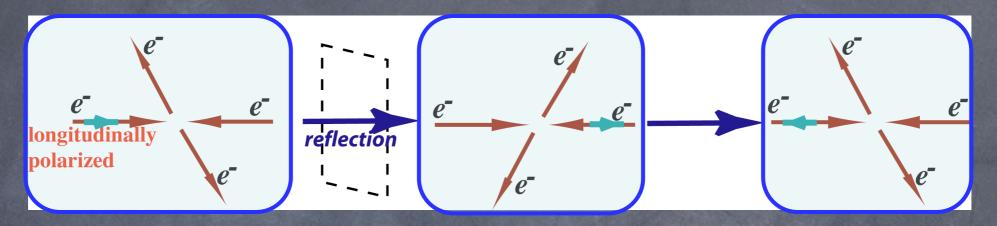
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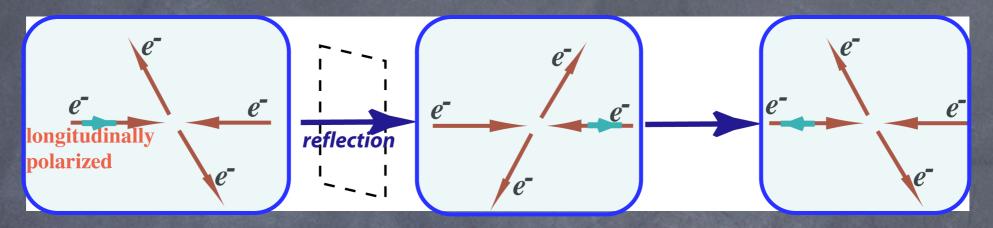


One of the incident beams longitudinally polarized Change sign of longitudinal polarization Measure fractional rate difference



One of the incident beams longitudinally polarized Change sign of longitudinal polarization Measure fractional rate difference

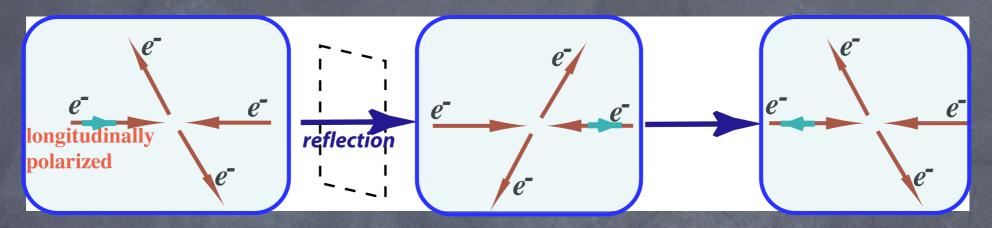
The matrix element of the Coulomb scattering is of the order of magnitude e^2/k^2 , where k is the momentum transferred ($\hbar = c = 1$). Consequently, the ratio of the interference term to the Coulomb term is of the order of gk^2/e^2 . Substituting $g = 10^{-5}/M^2$, where M is the mass of the nucleon, we find that for $k \sim M$ the parity nonconservation effects can be of the order of 0.1 to 0.01 percent.



One of the incident beams longitudinally polarized Change sign of longitudinal polarization Measure fractional rate difference

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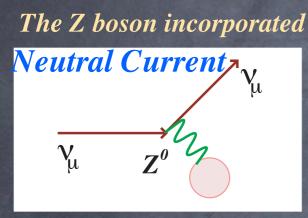
The idea could not be tested for 2 decades: Several circumstances aligned to make this an important measurement

Parity-violating electron scattering

29

Weak Interaction Theory

A Model of Leptons Steve Weinberg - 1967



Gargamelle finds one $v_{\mu} e^{-}$ event in 1973! (two more by 1976)



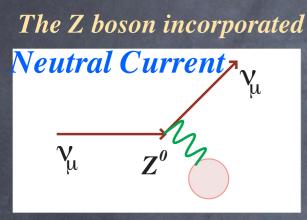
One free parameter: the weak mixing angle θ_W introduced

If θ_W were strictly zero, W & Z bosons would weigh exactly the same and right-handed particles would not exchange Z bosons either

	Left-	Right-
γ Charge	$0,\pm 1,\pm \frac{1}{3},\pm \frac{2}{3}$	$0,\pm 1,\pm \frac{1}{3},\pm \frac{2}{3}$
W Charge	$T = \pm \frac{1}{2}$	zero
Z Charge	$T - q\sin^2\theta_W$	$-q\sin^2\theta_W$

Weak Interaction Theory

A Model of Leptons Steve Weinberg - 1967



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Neutrino scattering measurements find θ_W is non-zero

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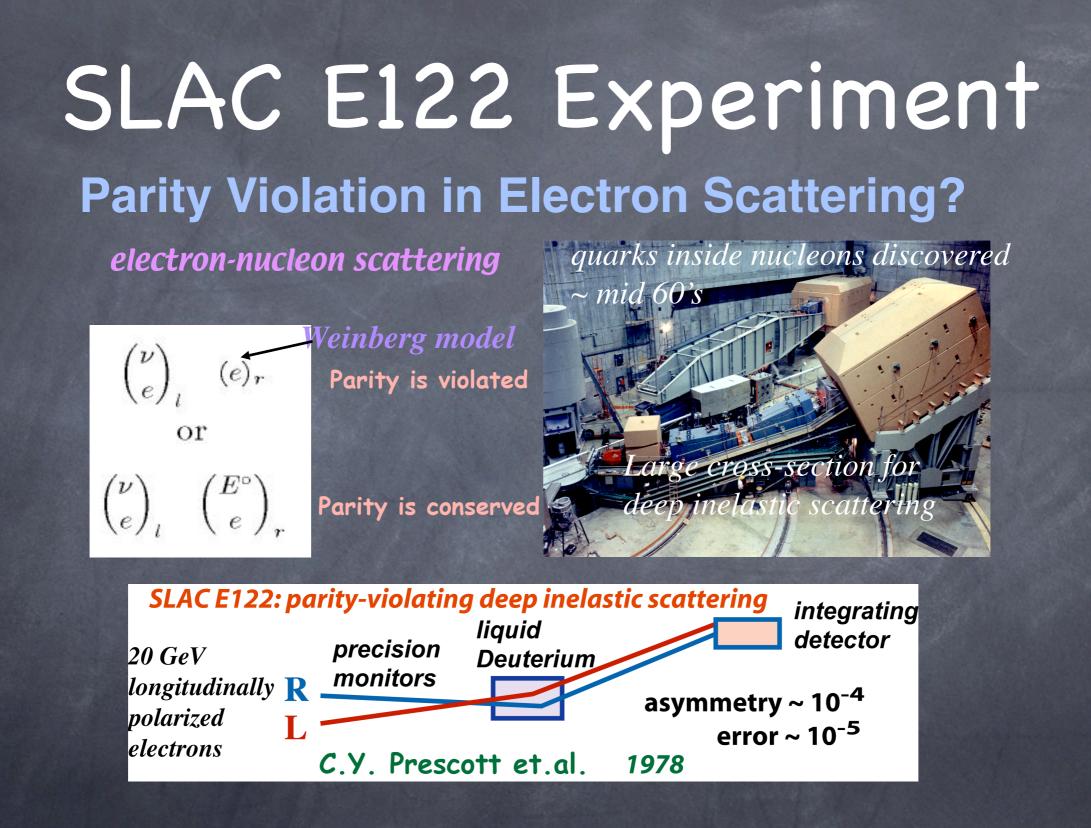
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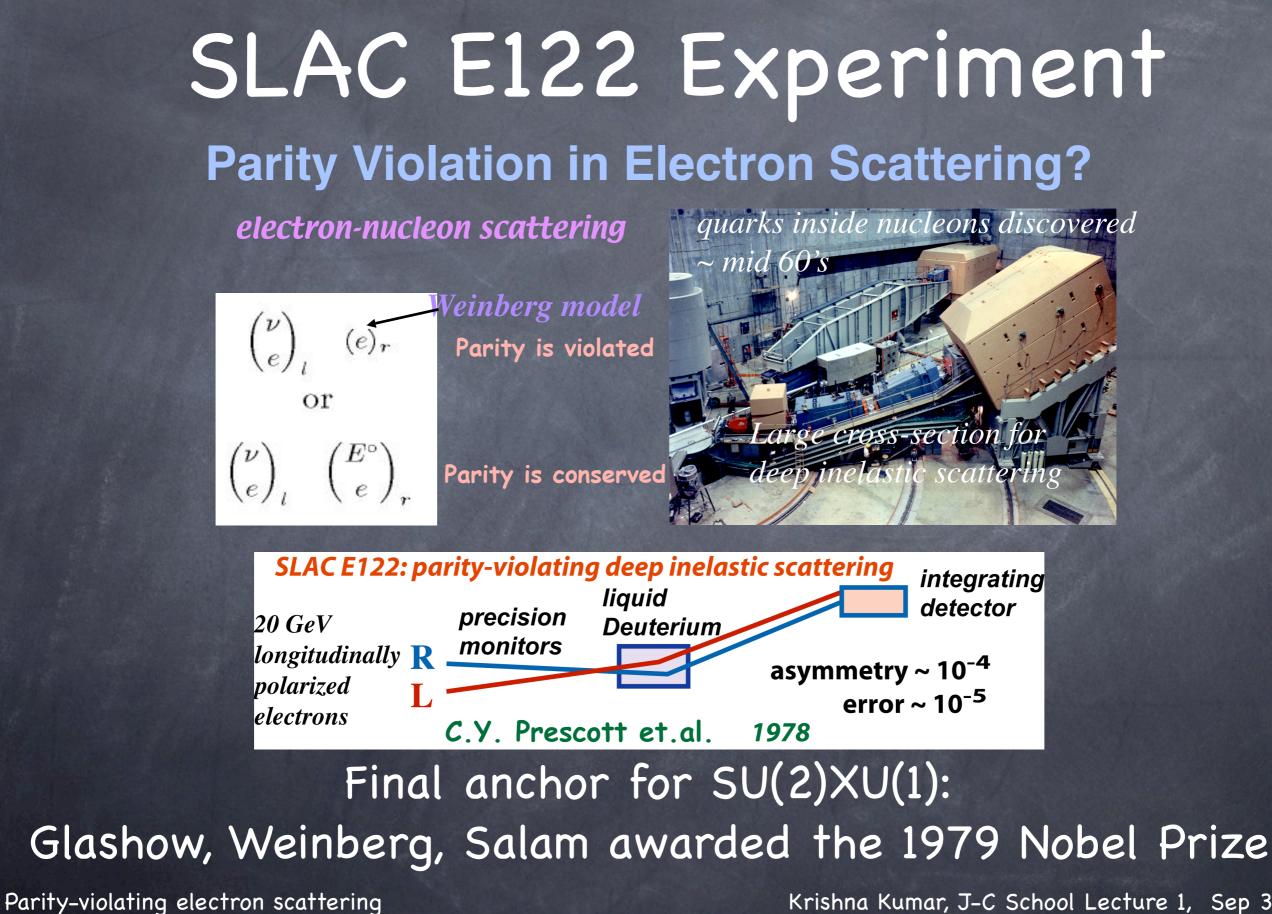
SLAC E122 Experiment **Parity Violation in Electron Scattering?** electron-nucleon scattering

 $\begin{pmatrix} \nu \\ e \end{pmatrix}_{l} \quad \stackrel{(e)_{r}}{(e)_{r}} \quad Parity is violated$ or $\begin{pmatrix} \nu \\ e \end{pmatrix}_l \quad \begin{pmatrix} E^\circ \\ e \end{pmatrix}_r$ Parity is conserved

Parity-violating electron scattering

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Summary

A very successful theoretical framework exists to describe electroweak interactions over a wide range of energy scales

Neutral weak interactions can be used to probe novel aspects of hadron structure

Parity-violating electron scattering is the ideal tool to probe low energy neutral weak interactions

Parity-violating electron scattering

Lecture 2 Overview

Strange Quark Content of the Nucleon The HAPPEX and HAPPEXII experiments The Neutron Skin of a Heavy Nucleus The PREX Experiment Future Program of Parity-violating Electron Scattering