


 norbplace:

- Experimental overview of some nuclei, after all the theory
- Theorists.... Please interrupt and explain, if you like
- Rather light nuclei....
- Olivier will cover the heavier nuclei, later
- No equations, but some interesting phenomena...











4-proton system doesn't exist... proton repulsion and Pauli effects

"Maximally symmetric" alpha-particle has a particularly high binding energy


Could a 4-neutron system exist...? no repulsion but still have Pauli effects "Tetraneutron"



There is no stable mass $A=5$ system


The resonances have asymmetric shapes due to the changing barrier penetrability as a function of the relative energy (alpha-nucleon) AND
The lineshape
depends on the production method, e.g. stripping from ${ }^{6} \mathrm{Li}$ or pickup onto ${ }^{4} \mathrm{He}$
C. L. Woods, F. C. Barker, ${ }^{\text {A W. W. Catford, L. K. Fifield and N. A. Orr }}$




This is unbound, but observable as a low-lying resonance, and is the $T_{z}=-1$ analog of $T_{z}=1$ weakly bound nucleus ${ }^{6} \mathrm{He}$

Unbound by 1.372 MeV to $\alpha+\mathrm{p}+\mathrm{p}$, Width of $0^{+}$ground state resonance $=92 \mathrm{keV}$, $(\mathrm{h} / 2 \pi) /$ width $=\left(6.578 \times 10^{-22} \mathrm{MeV} . \mathrm{s}\right) / 0.092 \sim 10^{-20} \mathrm{~s}$

Weakly bound, $\mathrm{S}_{\mathrm{n}}=1.867 \mathrm{MeV}$ ( $\mathrm{S}_{\mathrm{p}}=26.52 \mathrm{MeV}$ )
( $\beta$-decays, half-life $=806.7 \mathrm{~ms}$ )

Neutron skin, or halo


Structure of unbound system revealed by decay kinematics





Double-hump from (0p) ${ }^{2}$ structure, Sensitivity to model parameters.



## These $\mathrm{A}=7$ nuclei are well described as orbiting clusters of $\alpha+{ }^{3} \mathrm{He} / 3 \mathrm{H}$

A "few-body model" (here, two-body) works very well, using free-space properties of the two clusters, after including Pauli approximately with nodal requirements. (Fully antisymmetrized models also exist, of course, e.g. RGM, Brink model) (Most cluster models do include full antisymmetrization.)


## B Buck $\dagger$ and A C Merchant

J. Phys. G: Nucl. Phys. 14 (1988) L211-L216|

The essence of this model is to describe ${ }^{7} \mathrm{Li}$ and ${ }^{7} \mathrm{Be}$ as $\alpha-{ }^{3} \mathrm{H}$ and $\alpha-{ }^{3} \mathrm{He}$ systems respectively, with the clusters having essentially unperturbed free space properties. The cluster core interaction is taken to have a Gaussian form, and its parameters are determined unambiguously from the experimentally measured properties of ${ }^{7} \mathrm{Li}$ and ${ }^{7} \mathrm{Be}$. The relation of this elementary cluster model to the microscopic RGM has recently been investigated by Walliser and Fliessbach (1985), who conclude that as a model of ${ }^{7} \mathrm{Li}$ it is valid and useful, with a similar degree of justification to that of the nucleon picture of the deuteron.

| Quantity | Experimental values | This calculation |
| :---: | :---: | :---: |
| $\begin{aligned} & \left\langle r_{\mathrm{c}}^{2}\right\rangle^{1 / 2} \\ & (\mathrm{fm}) \end{aligned}$ | $2.41 \pm 0.10^{\text {c }}$ | $2.43 \pm 0.02$ |
| $\frac{Q}{\left(\mathrm{e} \mathrm{fm}^{2}\right)}$ | $\begin{gathered} -4.06 \pm 0.03^{d} \\ -3.70 \pm 0.08^{\mathrm{d}} \\ -4.0 \pm 1.1^{\mathrm{d}} \end{gathered}$ | $-3.83 \pm 0.13$ |
| $\begin{aligned} & B(\mathrm{E} 2 ; \uparrow) \\ & \left(e^{2} \mathrm{fm}^{4}\right) \end{aligned}$ | $\begin{aligned} 8.9 & \pm 0.6^{\mathrm{d}} \\ 8.3 & \pm 0.5^{\mathrm{e}} \\ 7.42 & \pm 0.14^{\mathrm{l}} \\ 6.7 & \pm 0.2^{\mathrm{g}} \\ 7.4 & \pm 0.1^{\mathrm{h}} \\ 8.3 & \pm 0.6^{i} \end{aligned}$ | $7.75 \pm 0.50$ |
| $\begin{aligned} & \left\langle r_{i n}^{2}\right\rangle^{1 / 2} \\ & (\mathrm{fm}) \end{aligned}$ | $\begin{aligned} & 2.98 \pm 0.05^{z} \\ & 2.70 \pm 0.15^{\mathrm{j}} \end{aligned}$ | $2.78 \pm 0.03$ |
| $\begin{aligned} & \Omega / \mu_{7} \\ & (\mathrm{fm})^{2} \end{aligned}$ | $\begin{aligned} & \pm 2.9 \pm 0.1^{\mathrm{g}} \\ & \pm 2.8 \pm 0.5^{\mathrm{i}} \end{aligned}$ | $-2.48 \pm 0.08$ |
| $S_{0}$ <br> ${ }^{3} \mathrm{He}(\alpha, \gamma){ }^{7} \mathrm{Be}$ <br> ( keV b) | $\begin{aligned} & 0.47 \pm 0.02^{k} \\ & 0.53 \pm 0.03^{\prime} \\ & 0.63 \pm 0.04^{\mathrm{m}} \\ & 0.51 \pm 0.05^{\mathrm{n}} \\ & 0.47 \pm 0.05^{\circ} \end{aligned}$ | $0.51 \pm 0.03$ |
| $\mathrm{d} S /\left.\mathrm{d} E\right\|_{\mathrm{G}}(\mathrm{mb})$ | $-0.28 \pm 0.04^{\text {n }}$ | $-0.27 \pm 0.04$ |
| $S_{0}$ | $0.100 \pm 0.025^{P}$ | $0.089 \pm 0.030$ |
| $\begin{aligned} & { }^{3} \mathrm{H}(\alpha, \gamma)^{7} \mathrm{Li} \\ & (\mathrm{keV} \mathrm{~b}) \end{aligned}$ | $0.134 \pm 0.020^{4}$ |  |
| $\mathrm{d} S /\left.\mathrm{d} E\right\|_{0}(\mathrm{mb})$ |  | $-0.18 \pm 0.04$ |



Three- $\alpha$ cluster state Is not the ground state $\mathrm{E}_{\mathrm{x}}=7654 \mathrm{keV}$
$\mathrm{E}_{\text {rel }}=287.55 \mathrm{keV} \alpha+{ }^{8} \mathrm{Be}$ Width $=8.5 \mathrm{eV}$ (some $\gamma$ !) (h/2p)/width ~ 0.1 fs $B E / A=7.04 \mathrm{MeV}$

## ${ }^{8} \mathrm{Be}$

Although it consists of two $\alpha$-particles, 8Be itself is not bound

$\mathrm{E}_{\text {rel }}=92 \mathrm{keV}$ to $\alpha+\alpha$
Width $=5.57 \mathrm{eV}$, $(\mathrm{h} / 2 \pi) /$ width $\sim 0.1 \mathrm{fs}$ $\mathrm{BE} / \mathrm{A}=7.06 \mathrm{MeV} / \mathrm{A}$

In summary, close to threshold we tend to see states with cluster structure... (see Ikeda diagram...)


In either the deformed Harmonic Oscillator or the two centre Harmonic Oscillator,
The energy of the second 4 nucleons drops with deformation
This pushes towards deformation until surface tension limits the deformation


The projection of the matter density In a DHO or TCHO shows "clusters"

[^0]


The sum of the $2 \Psi$ quartet densities (one even, one odd parity) shows a dip indicating clustering.

An alternative linear combination of wave functions $\Phi$ highlights the clustering


Clustering emerges naturally in Antisymmetrised Molecular Dynamics In which there are independent nucleons with no assumed clustering, Here we see the predicted matter density for all beryllium isotopes shown from ${ }^{6} \mathrm{Be}$ to ${ }^{14} \mathrm{Be}$
On the left, total intrinsic matter density, then proton density, then neutron density


"Excitation energy" spectrum of ${ }^{8} \mathrm{Be}$ deduced from energies of deuterons from

## ${ }^{9} \mathrm{Be}(\mathrm{p}, \mathrm{d})^{8} \mathrm{Be}$

"Spatial localisation anomaly" in ${ }^{9} \mathrm{Be}(\mathrm{p}, \mathrm{d})^{8} \mathrm{Be}(\alpha) \alpha$ E.H. Beckner et al, Phys. Rev. 123 (1961) 255
F. C. BARKER AND P. B. TREACY Nuclear Physics 38 (1962) 33-49

## Ghosts



> Gioster


As was pointed out by Beckner et al. ${ }^{3}$ ) the plateau at an excitation energy of about 1 MeV in the cross section for the reaction $\mathrm{Be}^{9}\left(\mathrm{p}\right.$, d) $\mathrm{Be}^{8}(\alpha) \mathrm{He}^{4}$ is due to transitions through the $\mathrm{Be}^{8}$ ground state. The ground state contribution, shown in fig. 1 , has two peaks, the one corresponding to a $\mathrm{Be}^{8}$ excitation $E \approx E_{\S}=0.094 \mathrm{MeV}$ and the other to $E \approx 1 \mathrm{McV}$. Such a bebaviour is expected for aill wectons on the
in which $\mathrm{Be}^{8}$ occurs as the intermediate nucleus. However, usually the upper peak will be masked by the tail of the contribution from the 2.9 MeV state of $\mathrm{Be}^{8}$ (as for
 (1) similar anomalous peaks, or "ghosts", might be expected in the spectra of excitation energies of nuclei B for which a level, well separated from other levels of the same spin and parity, exists close to a threshold, so that in an energy region above threshold the 自 same reason, similar ghosts might appear in the cross section for a normal resonance reaction

$$
A+a \rightarrow B \rightarrow C+c
$$

provided B has an isolated level near enough to either the $(A+a)$ or the $(C+c)$ threshold.
"Spatial localisation anomaly" in ${ }^{9} \mathrm{Be}(\mathrm{p}, \mathrm{d})^{8} \mathrm{Be}(\alpha) \alpha$ E.H. Beckner et al, Phys. Rev. 123 (1961) 255
F. C. BARKER AND P. B. TREACY Nuclear Physics 38 (1962) 33-49


Ghost of 7.654 MeV in ${ }^{12} \mathrm{~B} \beta$-decay


Ghost seen as resonance in $p+{ }^{11} B$


Fig. 3. Density-of-states function $\rho_{0}{ }^{(1)}(E)$ associated with the break-up of the 7.66 MeV state of $\mathrm{C}^{1}$ Fig. 4. Density-of-states function $\rho_{1}{ }^{(1)}(E)$ associated with the break-up of the 16.11 MeV state of $\mathrm{C}^{1}{ }^{1}$ into $\mathrm{Be}^{8}+\alpha$, as a function of channel energy $E$. The dotted portion of the curve corresponds to th into $\mathrm{B}^{11}-\mathrm{p}$, as a function of channel energy $E$. The dotted portion of the curve corresponds to the 7.66 MeV peak with a width of 8 eV and a height of $4 \times 10^{3}$. The curve labelled $\rho W^{5}$ gives the yield o 16.11 MeV peak with a width of 5 keV and a height of 100 . The curve labelled $\rho / E$ gives the cross $\mathrm{C}^{12}$ from the $\beta$-decay of $\mathrm{B}^{12}, W$ being the available $\beta$-energy.
section for the reaction $\mathrm{B}^{11}(\mathrm{p}, \alpha) \mathrm{Be}^{s}$ due to this state.

## F. C. BARKER AND P. B. TREACY Nuclear Physics 38 (1962) 33-49


${ }^{9} \mathrm{~B}$ has no bound states and a key question is the energy of the $1 / 2+$ state that is predicted but for which there is a lot of poor quality data.
${ }^{9} \mathrm{~B}$ to ${ }^{8} \mathrm{Be}+\mathrm{p} 185 \mathrm{keV}$
${ }^{9} \mathrm{~B}$ to $\alpha+\alpha+\mathrm{p} 278 \mathrm{keV}$ Width $=0.54 \mathrm{keV}, \sim 10^{-18} \mathrm{~s}$

${ }^{9}$ Be has a remarkable "nuclear molecule" structure based on two $\alpha$-particles and a valence neutron

## ${ }^{9} \mathrm{He}$

${ }^{9} \mathrm{He}$ is unbound and very neutron rich.
It can be observed as a resonance in the ${ }^{8} \mathrm{He}+\mathrm{n}$ system.
(is there level inversion like ${ }^{11} \mathrm{Be}$ ?)
(1/2+ below 1/2- ?)


A favourite of Alex Brown, but in fact it proves the existence of nuclear cluster states...

... this turns out to be a successful prediction for ${ }^{10} \mathrm{Be}$ (see later)
${ }^{9} \mathrm{He}: \mathrm{C}\left({ }^{11} \mathrm{Be},{ }^{8} \mathrm{He}+\mathrm{n}\right) @ 35 \mathrm{MeV} /$ nucleon

$s$-wave $\left[a_{s}=-3 \sim 0 \mathrm{fm}(3 \sigma)\right]+$ non-resonant continuum
H Al Falou LPCC 07-03

H. Al Falou, N.A. Orr, et al.

CHARISSA+DEMON at GANIL
Reconstruct $\mathbf{E}_{\text {rel }}\left({ }^{8} \mathrm{He}+\mathbf{n}\right)$ from measured angles and energies

Some evidence for persistence of $\mathbf{1 s}_{1 / 2}$ and $0 p_{1 / 2}$ level inversion as seen in ${ }^{11} \mathrm{Be}$ and ${ }^{10} \mathrm{Li}$


$$
{ }^{6} \mathrm{Li}\left({ }^{6} \mathrm{Li}, \mathrm{~d}\right){ }^{10} \mathrm{~B}(\mathrm{n}){ }^{9} \mathrm{~B}^{*}(\mathrm{p})^{8} \mathrm{Be}(\alpha) \alpha
$$

n
reconstructed

Ground state is $3 / 2^{-}$
The $1 / 2^{+}$state can be compared to the ${ }^{9} \mathrm{Be}$ mirror (Thomas-Ehrman shift) (both are unbound for $\mathrm{A}=9$ )

Controversial...

- identity
- energy
- seems to be "too low"

PHYSICAL REVIEW


An Analysis of the Energy Levels of the Mirror Nuclei, $\mathbf{C}^{13}$ and $\mathbf{N}^{13}$

Kellogg Radiation Laboratory, California Institue of Technology, Pasadena, California


${ }^{10} \mathrm{C}$ is the analog of ${ }^{10} \mathrm{Be}$, with two protons replacing two valence neutrons - do the same structures exist?

One bound excited $2^{+}$state

${ }^{10} \mathrm{Be}$ shows molecular structure, but mostly in the excited states.


Fig. 30. The intrinsic structure of the excited states of ${ }^{10} \mathrm{Be}$ obtained by VAP calculations. The density distribution of matter, protons and neutrons of the intrinsic states are shown at left, middle and right, respectively. The density is integrated along the axis perpendicular to adequate planes. The figures are for the results with the interaction (g).
Y. Kanada-En'vo and H. Horiuch 1

Progress of Theoretical Physics Supplement No. 142, 2001

(a) $\pi$ bond
(b) $\sigma$ bond

Microscopic cluster model (as for ${ }^{6} \mathrm{He}$ earlier)




Rep. Prog. Phys. 70 (2007) 2149-2210
Martin Freer


Super- Borromean... "Brunnian"

## ${ }^{10} \mathrm{C} @ 10.7 \mathrm{MeV} / \mathrm{A}$ on ${ }^{9}$ Be Texas A\&M


R. J. CHARITY et al.|

PHYSICAL REVIEW C 75, 051304(R) (2007)|
${ }^{10} \mathrm{C} @ 33.3 \mathrm{MeV} / \mathrm{A}$ on ${ }^{12} \mathrm{C}$ GANIL

N. CURTIS et al.

PHYSICAL REVIEW C 77, 021301(R) (2008)|



Weakly bound $\mathrm{S}_{\mathrm{n}}=0 . \mathrm{xx} \mathrm{MeV}$
Halo nucleus

This is a classic single-neutron halo nucleus,
 where the weak binding automatically leads to a halo

Both the intruder $1 / 2^{+}$ground state and the low $1 / 2^{-}$state have a halo - despite the centrifugal barrier for the $\mathrm{p}_{1 / 2}$ state.

The halo is not pure, however, and there is a component of the ground state in which the deformed core is excited to $2^{+}$ and a d-wave neutron is coupled to give spin $1 / 2$.

Weakly bound $\mathrm{S}_{\mathrm{n}}=0 . \mathrm{xx} \mathrm{MeV}$
Halo nucleus

# Structure of unstable light nuclei 

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Nuclear Physics A 693 (2001) 394-410|

## Abstract

The structure of light nuclei out to the drip lines and beyond up to $Z \sim 8$ is interpreted in terms of the shell model. Special emphasis is given to the underlying supermultiplet symmetry of the $p$-shell nuclei which form cores for neutrons and protons added in $s d$-shell orbits. Detailed results are given on the wave functions, widths, and Coulomb energy shifts for a wide range of non-normal parity states in the $p$-shell. © 2001 Elsevier Science B.V. All rights reserved.

## Lasers take a measure of halo nucleus

Mar 9, $2009 \square$ comments
physicsworld.com


Halo nucleus
Physicists in Europe and North America have measured the radius of an unusual beryllium isotope containing a single neutron a long way from the rest of the nuclear core. Although the radii of other such "halo" isotopes have been determined before, this is the first time that the measurement has been made on a nucleus with just a single halo neutron. The researchers found that the halo neutron in beryllium-11 is, on average, about $7 \mathrm{fm}\left(7 \times 10^{-15} \mathrm{~m}\right)$ from the nuclear core, which itself has a radius of about 2.5 fm .

## Measurements and calculations

The new study was carried out at the ISOLDE facility at CERN by Wilfried Nörtershäuser at the University of Mainz and colleagues in Germany, Canada and Switzerland (Phys. Rev. Lett. 102062503 ).

The experiment involved producing four different isotopes of beryllium (with 7,910 and 11 nucleons) by firing a 1.4 GeV proton beam into a uranium-carbide target. This created beryllium atoms, which were then ionized using a laser and accelerated to 50 kV . Transitions in electron energy levels were induced by firing two ultraviolet laser beams at the ions. One beam was fired straight at the oncoming ions, while the other was fired in the opposite direction from behind the ions to cancel out the experimental uncertainty in the kinetic energy of the ions.

Measuring ${ }^{11} \mathrm{Be}$ structure as superposition of $1^{0} \mathrm{Be}\left(0^{+}\right)+v\left(\mathrm{~s}_{1 / 2}\right)$ and ${ }^{10} \mathrm{Be}\left(2^{+}\right)+v\left(\mathrm{~d}_{5 / 2}\right)$

Removal of last neutron via ( $\mathrm{p}, \mathrm{d}$ ) transfer
J.S. Winfield et al. / Nuclear Physics A 683 (2001) 48-78|
S. Fortier et al. / Physics Letters B 461 (1999) 22-27


## 11 Be



## Focal plane spectrum from SPEG magnetic spectrometer



Separation Energy form factor



$\left\{\begin{array}{lr}0.74 & 0.19 \\ \text { Shell model }\end{array}\right\}$

[^1]
${ }^{14} \mathrm{C}$ is magic -
p3/2 protons closed p1/2 neutrons closed
N=8 closure is good
$S_{p}=20.832 \mathrm{MeV}$
$S_{\mathrm{n}}=8.177 \mathrm{MeV}$
$S_{\alpha}=12.012 \mathrm{MeV}$
(see next slide)

${ }^{12}$ Be sees a total collapse of magicity.. just by the...
...removal of two protons but keeping $\mathrm{N}=8$

Excited states in ${ }^{12} \mathrm{Be}$ seem to show ${ }^{6} \mathrm{He}+{ }^{6} \mathrm{He}$ clustering behaviour.




$\mathrm{He}-6$
M. Freer et al., Phys. Rev. Lett., 82 (1999) 1383

Ground state - a more normal deformation, Excited band - 2:1 ${ }^{6} \mathrm{He}+{ }^{6} \mathrm{He}$ cluster configuration

## But note :

$\mathrm{He}-6$


PHYSICAL REVIEW C 76, 064313 (2007)
R. J. CHARITY et al.|


Both ${ }^{13} \mathrm{Be}$ and ${ }^{10} \mathrm{Li}$ are unbound sub-systems of bound halo systems ( ${ }^{14} \mathrm{Be}$ and ${ }^{11} \mathrm{Li}$ )


If we remove a single neutron from the bound halo system And then observe the other neutron and the core nucleus, And then reconstruct the relative momentum...

Do we measure the neutron-core interaction in an accurate manner, or do we observe some vestige of the structure in the original halo...?

How well do reconstructed resonances in the sub-system resemble the actual sub-system and how much are they a remnant of the initial state? Are standard resonance line-shapes expected? .... (YES)


Calculated reaction products compared with resonances

## ${ }^{13} \mathrm{Be}$

FIG. 7. The ${ }^{11} \mathrm{Li} 1 n$-stripping energy distributions in the norecoil transparent limit (solid curves) are compared to fits obtained from Eq. (20) and Eqs. (21) and (22) (dashed curves). Shown are the $s$ - and $p$-wave components of the $s 23$ wave function.


FIG. 6. Percentage of $s$ and $p$ waves in the various models, comparing the probabilities in the wave functions (wf) to the probabilities in the neutron-core final states $(\sigma)$.
G. F. BERTSCH, K. HENCKEN, AND H. ESBENSEN PRC 37 (1998) 1366

(see next slide) $\longleftarrow \longleftarrow \begin{aligned} & \text { Borromean halo nucleus } \\ & \mathrm{S}_{2 \mathrm{n}}=1.12 \mathrm{MeV}\end{aligned}$
${ }^{12} \mathrm{Be}_{\mathrm{n}}=3.17 \mathrm{MeV}$

There may be a component of the ground state that has this structure, which may account for the observation of the "tetraneutron" events (possible 4 n resonance?)

rms separations for core and neutrons in few-body ${ }^{11} \mathrm{Li}$ model, compared to ranges of potentials M.V. Zhukov et al., Phys. Rep. 231, 151 (1993).

Interferometry between the two neutrons at GANIL/DEMON measures their rms separation in the ${ }^{14} \mathrm{Be}$ source


The interaction radius from total cross section
The interaction radius from total cross section
measurements is clearly larger for halo nuclei

14 Be

rms separations for core and neutrons in few-body ${ }^{11} \mathrm{Li}$ model, compared to ranges of potentials M.V. Zhukov et al., Phys. Rep. 231, 151 (1993).




[^0]:    M. Freer ${ }^{1}$, R.R. Betts, A.H. Wuosmaa

    Nuclear Physics A 587 (1995) 36-54

[^1]:    C.M. angle (deg)

