The Very Rich Structure of the Rather Light Nu

Wilton Catford

University of Surrey, Guildford, UK

Ecole Joliot Curie, September 2009

Photo: Coconuts Beach Resort Samoa (2005)

The Very Rich Structure of the Rather Light N

Wilton Catford

University of Surrey, Guildford, UK

Ecole Joliot Curie, September 2009

A.		EARTHQUAKE MAGNITUDE 8.3
FIJI	Pacific Ocean	
e ¹ v		TONGA

100 200km

SAMOA

AMERICAN



U.S. citizen Heather Penner, who works at Coconut Resort at Maninoa Siumu on the southern coast of Western Samoa walks through the remains of her Tsunami destroyed workplace.

- Experimental overview of some nuclei, after all the theory
- Theorists.... Please interrupt and explain, if you like
- Rather light nuclei....
- Olivier will cover the heavier nuclei, later
- No equations, but some interesting phenomena...





















4-proton system doesn't exist... proton repulsion and Pauli effects

Ω



"Maximally symmetric" alpha-particle has a particularly high binding energy





Could a 4-neutron system exist...? no repulsion but still have Pauli effects **"Tetraneutron"**





There is no stable mass A=5 system







This is unbound, but observable as a low-lying resonance, and is the $T_z = -1$ analog of $T_z = 1$ weakly bound nucleus ⁶He



Unbound by 1.372 MeV to α + p + p, Width of 0⁺ ground state resonance = 92 keV, (h/2 π)/width = (6.578×10⁻²² MeV.s)/0.092 ~ 10⁻²⁰ s



L.V. Grigorenko et al. / Physics Letters B 677 (2009) 30-35

Structure of unbound system revealed by decay kinematics





Double-hump from (0p)² structure, Sensitivity to model parameters.







These A=7 nuclei are well described as orbiting clusters of α + ³He/³H

A "few-body model" (here, two-body) works very well, using <u>free-space properties</u> of the two clusters, after including Pauli approximately with nodal requirements. (Fully antisymmetrized models also exist, of course, e.g. RGM, Brink model) (Most cluster models do include full antisymmetrization.)

⁷ Be	
	⁷ Li

B Buck† and A C Merchant J. Phys. G: Nucl. Phys. 14 (1988) L211–L216

The essence of this model is to describe ⁷Li and ⁷Be as α —³H and α —³He systems respectively, with the clusters having essentially unperturbed free space properties. The cluster core interaction is taken to have a Gaussian form, and its parameters are determined unambiguously from the experimentally measured properties of ⁷Li and ⁷Be. The relation of this elementary cluster model to the microscopic RGM has recently been investigated by Walliser and Fliessbach (1985), who conclude that as a model of ⁷Li it is valid and useful, with a similar degree of justification to that of the nucleon picture of the deuteron.

Quantity	Experimental values	This calculation
$\langle r_{\rm c}^2 \rangle^{1/2}$	$2.41\pm0.10^{\rm c}$	2.43 ± 0.02
(fm)		
\mathcal{Q}	-4.06 ± 0.03^{d}	-3.83 ± 0.13
(e fm ²)	$-3.70 \pm 0.08^{\circ}$	
	-4.0 ± 1.1^{f}	
$B(E2; \uparrow)$	$8.9\pm0.6^{ m d}$	7.75 ± 0.50
$(e^2 {\rm fm}^4)$	$8.3\pm0.5^{\circ}$	
	$7.42\pm0.14^{\circ}$	
	$6.7\pm0.2^{ m g}$	
	$7.4\pm0.1^{ m h}$	
	8.3 ± 0.6^{10}	
$\langle r_{\rm m}^2 \rangle^{1/2}$	$2.98\pm0.05^{\rm g}$	2.78 ± 0.03
(fm)	2.70 ± 0.15^{i}	
$\hat{\Omega}/\mu_7$	$\pm 2.9 \pm 0.1^{g}$	-2.48 ± 0.08
$(fm)^2$	\pm 2.8 \pm 0.5 ^j	
\hat{S}_{G}	0.47 ± 0.02^k	0.51 ± 0.03
3 He $(\alpha, \gamma)^{7}$ Be	$0.53 \pm 0.03^{\circ}$	
(keV b)	0.63 ± 0.04^{m}	
× ·	$0.51 \pm 0.05^{\circ}$	
	$0.47\pm0.05^{\circ}$	
$dS/dE _{e}$ (mb)	-0.28 ± 0.04^{n}	-0.27 ± 0.04
Sa	0.100 ± 0.025^{p}	0.089 ± 0.030
${}^{3}\mathrm{H}(\alpha, \gamma)^{7}\mathrm{Li}$	$0.134\pm0.020^{ m q}$	
(keVb)		
dS/dE_0 (mb)		-0.18 ± 0.04
10 (>		





In summary, close to threshold we tend to see states with cluster structure... (see lkeda diagram...)



New Scientist . www.newscientist.com

1 May 1999

In either the **deformed Harmonic Oscillator** or the **two centre Harmonic Oscillator**,

The energy of the second 4 nucleons drops with deformation This pushes towards deformation until

surface tension limits the deformation





The projection of the matter density In a DHO or TCHO shows "clusters"

M. Freer¹, R.R. Betts, A.H. Wuosmaa Nuclear Physics A 587 (1995) 36–54



The sum of the 2Ψ quartet densities (one even, one odd parity) shows a dip indicating clustering.

An alternative linear combination of wave functions Φ highlights the clustering



Clustering emerges naturally in Antisymmetrised Molecular Dynamics In which there are independent nucleons with **no assumed clustering**, Here we see the predicted matter density for all beryllium isotopes **shown from 6Be to 14Be**

On the left, total intrinsic matter density, then proton density, then neutron density





"Spatial localisation anomaly" in ${}^{9}Be(p,d){}^{8}Be(\alpha)\alpha$ E.H. Beckner et al, Phys. Rev. 123 (1961) 255



"Excitation energy" spectrum of ⁸Be deduced from energies of deuterons from

⁹Be(p,d)⁸Be

F. C. BARKER AND P. B. TREACY Nuclear Physics 38 (1962) 33-49



N COR

 $\rho_l^{(1)}(E) = \text{const.} \frac{\frac{1}{2}\Gamma_l}{(E_l + \Delta_l - E)^2 + (\frac{1}{2}\Gamma_l)^2},$ $\Gamma_1 = 2P_1\gamma_1^2, \qquad P_2 = \rho A_1^{-2},$ $\Delta_l = -S_l^0 \gamma_l^2, \qquad S_l^0 = \rho A_l^{-1} (\partial A_l / \partial \rho) - \mathbf{B}_l,$ $A_l^2 = F_l^2 + G_l^2.$ Eq. (4), E > 0

-S. ^{Ar}Cherrie

As was pointed out by Beckner *et al.*³) the plateau at an excitation energy of about 1 MeV in the cross section for the reaction $Be^9(p, d) Be^8(\alpha) He^4$ is due to transitions through the Be⁸ ground state. The ground state contribution, shown in fig. 1, has two peaks, the one corresponding to a Be⁸ excitation $E \approx E_c = 0.094$ MeV and the other to $E \approx 1$ MeV. Such a behaviour is expected for all reactions of the type

in which Be^8 occurs as the intermediate nucleus. However, usually the upper peak will be masked by the tail of the contribution from the 2.9 MeV state of Be^8 (as for example in the $B^{11}(p, \alpha) Be^8(\alpha)$ He⁴ reaction³)). In general for reactions of the type (1) similar anomalous peaks, or "ghosts", might be expected in the spectra of excitation energies of nuclei B for which a level, well separated from other levels of the same spin and parity, exists close to a threshold, so that in an energy region above threshold the numerator in eq. (4) is increasing more rapidly than the denominator. For the same reason, similar ghosts might appear in the cross section for a normal resonance reaction

$$A + a \rightarrow B \rightarrow C + c$$

provided B has an isolated level near enough to either the (A+a) or the (C+c) threshold.

"Spatial localisation anomaly" in ${}^{9}Be(p,d){}^{8}Be(\alpha)\alpha$ E.H. Beckner et al, Phys. Rev. 123 (1961) 255

F. C. BARKER AND P. B. TREACY Nuclear Physics 38 (1962) 33-49



Fig. 3. Density-of-states function $\rho_0^{(1)}(E)$ associated with the break-up of the 7.66 MeV state of C¹ Fig. 4. Density-of-states function $\rho_1^{(1)}(E)$ associated with the break-up of the 16.11 MeV state of C¹ into Be⁸+ α , as a function of channel energy *E*. The dotted portion of the curve corresponds to the into B¹¹-p, as a function of channel energy *E*. The dotted portion of the curve corresponds to the 7.66 MeV peak with a width of 8 eV and a height of 4×10^8 . The curve labelled ρW^5 gives the yield o 16.11 MeV peak with a width of 5 keV and a height of 100. The curve labelled ρ/E gives the cross C¹³ from the β -decay of B¹³, *W* being the available β -energy.

F. C. BARKER AND P. B. TREACY Nuclear Physics 38 (1962) 33-49



⁹B has no bound states and a key question is the energy of the 1/2+ state that is predicted but for which there is a lot of poor quality data.

⁹B to ⁸Be + p 185 keV ⁹B to α + α + p 278 keV Width = 0.54 keV, ~ 10⁻¹⁸ s



⁹Be has a remarkable "nuclear molecule" structure based on two α-particles and a valence neutron



⁹He is unbound and very neutron rich.
It can be observed as a resonance in the ⁸He + n system.
(is there level inversion like ¹¹Be?)
(1/2+ below 1/2-?)



A favourite of Alex Brown, but in fact it proves the existence of nuclear cluster states...



... this turns out to be a successful prediction for ¹⁰Be (see later)





H. Al Falou, N.A. Orr, et al.

CHARISSA+DEMON at GANIL

Reconstruct **E**_{rel}(⁸**He** + **n**) from measured angles and energies

Some evidence for persistence of $1s_{1/2}$ and $0p_{1/2}$ level inversion as seen in ¹¹Be and ¹⁰Li





Princeton University, Princeton, New Jersey



10C Lifetime = 19.3 s One bound excited 2+ state

¹⁰C is the analog of ¹⁰Be, with two protons replacing two valence neutrons – do the same structures exist ?



¹⁰Be shows molecular structure, but mostly in the excited states.

 $\rho/2$ ρ_n ρ_p 0^{+}_{1} 2^+_1 2^+_2 0^{+}_{2} 1 3 10 fm 10 fm 10 fm

Fig. 30. The intrinsic structure of the excited states of ¹⁰Be obtained by VAP calculations. The density distribution of matter, protons and neutrons of the intrinsic states are shown at left, middle and right, respectively. The density is integrated along the axis perpendicular to adequate planes. The figures are for the results with the interaction (g).

Y. Kanada-En'yo and H. Horiuchi Progress of Theoretical Physics Supplement No. 142, 2001 J. Phys. G: Nucl. Part. Phys. 24 (1998) 1499-1503.



(a) π bond

Koji Arai^{*} Department of Physics, University of Surrey, Guildford GU2 7XH,United Kingdom PHYSICAL REVIEW C **69**, 014309 (2004)

Microscopic cluster model (as for ⁶He earlier)





Koji Arai^{*} Department of Physics, University of Surrey, Guildford GU2 7XH,United Kingdom PHYSICAL REVIEW C 69, 014309 (2004)







0

0

0

 \bigcirc



Coexistence of THREE configurations

Necessary, to explain covalent molecular 0+









^{10}C @ 33.3 MeV/A on ^{12}C GANIL

N. CURTIS *et al.*

PHYSICAL REVIEW C 77, 021301(R) (2008)







This is a classic single-neutron halo nucleus, where the weak binding automatically leads to a halo

Both the intruder $1/2^+$ ground state and the low $1/2^-$ state have a halo – despite the centrifugal barrier for the $p_{1/2}$ state.

The halo is not pure, however, and there is a component of the ground state in which the deformed core is excited to 2⁺ and a d-wave neutron is coupled to give spin 1/2.



Nuclear Physics A 693 (2001) 394-410

Abstract

The structure of light nuclei out to the drip lines and beyond up to $Z \sim 8$ is interpreted in terms of the shell model. Special emphasis is given to the underlying supermultiplet symmetry of the *p*-shell nuclei which form cores for neutrons and protons added in *sd*-shell orbits. Detailed results are given on the wave functions, widths, and Coulomb energy shifts for a wide range of non-normal parity states in the *p*-shell. © 2001 Elsevier Science B.V. All rights reserved.

Lasers take a measure of halo nucleus

IOP A website from Institute of Physics Publishing

Mar 9, 2009 💷 2 comments



Physicists in Europe and North America have measured the radius of an unusual beryllium isotope containing a single neutron a long way from the rest of the nuclear core. Although the radii of other such "halo" isotopes have been determined before, this is the first time that the measurement has been made on a nucleus with just a single halo neutron. The researchers found that the halo neutron in beryllium–11 is, on average, about 7 fm (7 x 10⁻¹⁵ m) from the nuclear core, which itself has a radius of about 2.5 fm. **Measurements and calculations**

The new study was carried out at the ISOLDE facility at CERN by Wilfried Nörtershäuser at the University of Mainz and colleagues in Germany, Canada and Switzerland (*Phys. Rev. Lett.* **102** 062503).

The experiment involved producing four different isotopes of beryllium (with 7, 9 10 and 11 nucleons) by firing a 1.4 GeV proton beam into a uranium-carbide target. This created beryllium atoms, which were then ionized using a laser and accelerated to 50 kV. Transitions in electron energy levels were induced by firing two ultraviolet laser beams at the ions. One beam was fired straight at the oncoming ions, while the other was fired in the opposite direction from behind the ions to cancel out the experimental uncertainty in the kinetic energy of the ions.

physicsworld.com



Measuring ¹¹Be structure as superposition of $1^{0}Be(0^{+})+v(s_{1/2})$ and ${}^{10}Be(2^{+})+v(d_{5/2})$

Removal of last neutron via (p,d) transfer

J.S. Winfield et al. / Nuclear Physics A 683 (2001) 48–78 S. Fortier et al. / Physics Letters B 461 (1999) 22–27







Focal plane spectrum from SPEG magnetic spectrometer





Vibrational form factor





¹⁴C is magic –
p3/2 protons closed
p1/2 neutrons closed
N=8 closure is good

$$S_p = 20.832 \text{ MeV}$$

 $S_n = 8.177 \text{ MeV}$
 $S_{\alpha} = 12.012 \text{ MeV}$

(see next slide)



¹²Be sees a total collapse of magicity.. just by the...

...removal of two protons but keeping N=8

Excited states in ¹²Be seem to show ⁶He+⁶He clustering behaviour.









80

60 D

40

20 հյ

20

27.0

30

(c)

(b)

3





If we remove a single neutron from the bound halo system And then observe the other neutron and the core nucleus, And then reconstruct the relative momentum...

Do we measure the neutron-core interaction in an accurate manner, or do we observe some vestige of the structure in the original halo...?

How well do reconstructed resonances in the sub-system resemble the actual sub-system and how much are they a remnant of the initial state? Are standard resonance line-shapes expected? (YES)



FIG. 7. The ¹¹Li 1*n*-stripping energy distributions in the norecoil transparent limit (solid curves) are compared to fits obtained from Eq. (20) and Eqs. (21) and (22) (dashed curves). Shown are the *s*- and *p*-wave components of the *s*23 wave function.



FIG. 6. Percentage of *s* and *p* waves in the various models, comparing the probabilities in the wave functions (wf) to the probabilities in the neutron-core final states (σ).



For several structure models, comparison of relative peak strengths in reaction with relative strengths in the initial wavefunction

> G. F. BERTSCH, K. HENCKEN, AND H. ESBENSEN PRC 37 (1998) 1366



(see next slide) \blacksquare Borromean halo nucleus $S_{2n} = 1.12 \text{ MeV}$

 $^{12}\text{Be S}_{n} = 3.17 \text{ MeV}$





There may be a component of the ground state that has this structure, which may account for the observation of the "tetraneutron" events (possible 4n resonance?)





rms separations for core and neutrons in few-body ¹¹Li model, compared to ranges of potentials M.V. Zhukov *et al.*, Phys. Rep. **231**, 151 (1993).



The interaction radius from total cross section measurements is clearly larger for halo nuclei rms separations for core and neutrons in few-body ¹¹Li model, compared to ranges of potentials M.V. Zhukov *et al.*, Phys. Rep. **231**, 151 (1993).



The Very Rich Structure of the Rather Light Nu

Wilton Catford

University of Surrey, Guildford, UK

Ecole Joliot Curie, September 2009

Photo: Coconuts Beach Resort Samoa (2005)